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Privacy Preserving Identification: Order Statistics List Decoding Perspective

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Abstract—In this paper, the performance of privacy preserving Biometric/Physical Unclonable Function identification based on the order statistic list decoding is analyzed by evaluating the corresponding probabilities of correct identification and false acceptance. We demonstrate the impact of candidate list size on the identification system performance and compare it with the unique identification setup. Finally, the influence of privacy amplification on the system performance is analyzed.

Keywords—biometric identification; privacy amplification; list decoding; order statistics; correct identification; false acceptance; receiver operating characteristic.

I. INTRODUCTION

The present work addresses a privacy-preserving identification based on biometrics or Physical Unclonable Functions (PUFs). Both biometrics and PUFs are well-known in forensic applications [1] because of their ability to serve as a unique identifier for people and physical objects.

Design of biometric/PUF identification system is a complex optimization problem that is subject to a set of conflicting constraints. Leaving some of them, i.e., security and complexity, outside of the scope of this paper, we present a solution to a performance-privacy trade-off in such a design.

Because of channel distortions, due to acquisition imperfection, compression etc., the identification system should be able to cope with data degradations. In classical identification setups, the decoder estimates a unique index for a given query. Another approach, which can be considered as a generalization of the one mentioned above, firstly proposed by Elias [2] in information theory, is known as list decoding. The main feature of this type of decoding is to produce a fixed list size of the most likely candidates rather than a single one. The result of [2] was generalized by Forney to a variable list size [3]. In many identification problems, the final sink of information is a human being. This restriction makes variable list size decoding undesirable, due to the fact that in intensive degradation conditions the cardinality of candidates increases drastically.

A special care should be addressed to the organization of the system codebook/database. Specifically, even gaining the physical access to the storage module should not provide an unauthorized party with a privacy relevant information ready for a malicious misuse. The privacy of the entire protocol is usually ensured by following the principles of cryptographic privacy amplification (PA) [7]. Finally, an additional randomization of the database content might be proposed targeting further privacy strengthening.

Accordingly to such a strategy, the main contribution of this paper can be summarized as follows. We introduce the identification setup based on an order statistic list decoder (OSLD) of a fixed maximum list size and analyze its performance versus unique decoding. For reasons of computational complexity, privacy and security, it is undesirable for an identification system to retain the biometrics or PUFs in their original form. We use random projections and binarization for the digital fingerprint generation and channel statistics conversion to a binary model [5]. The applied mechanism of binary data generation additionally provides minimization of the privacy leakage to unauthorized parties. For additional privacy enforcement, a complementary randomization mechanism is exploited [7]. Finally, we analyze the OSLD probabilities of correct identification and false acceptance over the binary symmetric channel (BSC) for various privacy constraints.

Notations: We use capital letters $X$ to denote scalar random variables and $\mathbf{X}$ to denote vector random variables. Corresponding small letters $x$ and $\mathbf{x}$ denote the realizations of scalar and vector random variables. All vectors without sign tilde are assumed to be of the length $N$ and with the sign tilde of length $L$. $\mathcal{B}(N,p)$ denotes the Binomial distribution with $N$ trials and probability of success $p$. $V_{(r:M)}$ stands for the $r$-th order statistics of $M$ i.i.d. random variables.

II. IDENTIFICATION SETUP

The identification setup under analysis shown in Fig. 1 consists of two main phases: enrollment and identification. In the enrollment phase, the digital fingerprints of biometrics or PUFs of items to be identified $\mathbf{x}(m) \in \mathcal{X}^N, m = 1, \ldots, M$, which are drawn independently from a common stationary distribution $p_X(x)$, are stored in the Database. The digital fingerprints, which are short, robust and discriminative representative of items, are extracted in two steps. At the first step; by applying random projections [5], which are so-called orthoprojectors $\mathbf{W} \in \mathbb{R}^{L \times N}$ with $W_{ij} \sim \mathcal{N}(0, \frac{1}{N})$, $1 \leq i \leq L$ and $1 \leq j \leq N$, the dimensionality is reduced from $N$ to $L$. At the second
In the identification phase, for a given query \( Y \), which can be a noisy version of the biometrics or PUFs or originated from the data irrelevant to the stored in the database, the digital fingerprint is extracted following the same stages as in the enrollment phase, i.e., \( B_y = \Phi(Y) \), where \( Y = WY \).

Afterwards, the decoder detects that the query is related to some entries of the database, and if so, identifies to which ones.

The decoding process in the identification setup is accomplished in two steps. At the first step, the primary candidates are chosen by the OSLD. At the second step, a threshold is applied to all candidates, and the candidates which satisfy the constraint remain on the list. The decoding procedure can be summarized as follows:\(^1\):

1) The likelihood functions, \( p(y|x(m)) \), \( 1 \leq m \leq M \), for all database entries are computed.
2) The computed likelihood functions are sorted in ascending order.
3) The indices of the \( N_l \) largest likelihood functions are chosen which form the primary list \( N'_l \). The parameter \( |N'_l| = N_l \) is referred as a primary list size.
4) The final output set of the decoder is defined as \( N'_f = \{ m \in N'_l : p(y|x(m)) \geq e^{N_l} \gamma \} \) where the parameter \( \gamma \) controls the number of final candidates.

The performance of the decoder is evaluated by the probability of correct identification, i.e., \( P_c = \Pr\{m \in N'_l \cap |H_m| \} \), where \( H_m \) corresponds to \( Y \) related to the \( m^{th} \) entry of the database, and the probability of false acceptance, i.e., \( P_f = \Pr\{N'_f \neq \emptyset \| H_0 \} \), where \( H_0 \) corresponds to \( Y \) unrelated to any database entry.

\(^1\)The low-complexity identification of OSLD decoding based on the concept of bit reliability is given in [6].
is a decreasing function of the Hamming distance \( d(m) \equiv d_H(b_y, b_a(m)) \) for \( 0 \leq P_b \leq 0.5 \). In the following, we will consider the above Hamming distance as a realization of the random variable \( D(m) \) where \( m \) refers to the index of \( b_a(m) \). Given a query related to the \( m^{th} \) entry of the database, the event \( m \in N_l \) occurs, if \( d(m) \) is among the \( N_l \) smallest distances \( \{d(1), d(2), \ldots, d(M)\} \).

The dimensionality reduction and binarization modify the statistics of the database generated from \( p_X(x) \) to the Binomial distribution, i.e., \( B_{u}(m) \sim B(L, 1/2) \) for any \( p_X(x) \) with a diagonal covariance matrix.

Conditioned on \( \mathcal{H}_1 \), the sufficient statistics can be expressed as follows:

\[
D(m) \sim \begin{cases} 
B(L, P_{b_a}), & \text{for } m = 1, \\
B(L, \frac{1}{2}), & \text{for } m \neq 1.
\end{cases}
\]  

From (1), the complement of the CDF, \( F_N^{(N_l; M-1)}(d) \), of \( N_l^{th} \) order statistics of the i.i.d random variables \( D(m) \), \( m \neq 1 \) is given by:

\[
F_N^{(N_l; M-1)}(d) = \Pr\{D_{(N_l; M-1)} > d\} = \sum_{p=0}^{N_l-1} \binom{M-1}{p} s(d)^p(1-s(d))^{(M-1)-p},
\]  

where \( s(d) \equiv \sum_{x=0}^{d} \binom{L}{p} \left(\frac{1}{2}\right)^L \). From (5) and (6), the probability of correct identification (3) over the BSC can be expressed by:

\[
P_c(\alpha) = \Pr\{(D_{(N_l; M-1)} > D(1)) \cap (D(1) \leq \eta) | \mathcal{H}_1 \} = \sum_{d=0}^{\eta} \Pr\{D_{(N_l; M-1)} > d | \mathcal{H}_1, D(1) = d\} p_{D(1)}(d) = \sum_{d=0}^{\eta} \left\{ \sum_{p=0}^{N_l-1} \binom{M-1}{p} s(d)^p(1-s(d))^{(M-1)-p} \right\} \]

where from (3) and (4) \( \eta = L \frac{\gamma - \ln(1-P_{b_a})}{\ln P_{b_a}/(1-P_{b_a})} \), \( \alpha \) follows from (3) and the fact that the likelihood function is a decreasing function of the Hamming distance, and \( p_{D(1)}(d) \) denotes the PMF of \( D(1) \).

V. PROBABILITY OF FALSE ACCEPTANCE

The main reason to consider the probability of false acceptance is to show the reliability of the decoding process with respect to various attacking strategies. There are different scenarios to investigate the reliability of the decoder in identification setups:

- The PDF of database generation is known.
- The PDF of database generation is not known.

- The database entries are partially known.
- The database entries are totally known.

In this paper, we consider the scenario in which the PDF is fully known by the attacker. In the following, the false acceptance event is analyzed over the BSC according to the justification presented above.

To evaluate the probability of false acceptance, we define the following events:

\[
E_{D(i; M)} = \{ D(i; M) \leq \eta | \mathcal{H}_0 \},
\]

where \( 1 \leq i \leq N_l, D(m) \sim B(L_i, 1/2), 1 \leq m \leq M \), and \( E_{D(i; M)} \) is the event that the \( i^{th} \) ascending ranked Hamming distance between the query and an entry of database is smaller than the threshold. From (1), the probability of false acceptance is found as:

\[
P_f = \Pr\left\{ \bigcup_{i=1}^{N_l} E_{D(i; M)} | \mathcal{H}_0 \right\} = 1 - \Pr\left\{ \bigcap_{i=1}^{N_l} E_{D(i; M)}^c | \mathcal{H}_0 \right\}
\]

\[
(a) = 1 - \Pr\left\{ E_{D(1; M)}^c | \mathcal{H}_0 \right\} = \Pr\{ E_{D(1; M)} | \mathcal{H}_0 \}
\]

where \( E_{D(1; M)}^c \) is the complement of \( E_{D(i; M)} \) and \( (a) \) follows from the fact that as the event \( E_{D(1; M)}^c \) occurs the rest events occur. From (1), the probability of false acceptance can be computed by:

\[
P_f = \Pr\left\{ \min_{1 \leq m \leq M} D(m) \leq \eta | \mathcal{H}_0 \right\} = 1 - \left[ 1 - \sum_{x=0}^{\eta} \binom{L}{x} \left(\frac{1}{2}\right)^L \right]^M.
\]

The interesting point to note is that the probability of false acceptance is unexpectedly independent of the primary list size.

VI. SIMULATION RESULTS

Without loss of generality, as it is mentioned before the identification is performed in the space of binary templates. Therefore, we will assume that the database entries can be represented by the Binomial distribution. Thus, the performance of the proposed decoder is evaluated by using databases of synthetic data with different sizes that are independently and identically distributed according to \( B_x \sim B(L_i, 1/2) \) that is as well optimal from a privacy point of view. The input to the identification system is obtained at the output of the BSC with a crossover probability \( P_{b_x} = P_b \ast \lambda = P_b \ast \left(\frac{1}{\pi} \arccos \rho_x \right) \) [6], where \( \rho_x \) is a cross-correlation coefficient between \( X \) and \( Y \). Fig. 2 confirms the accuracy of the derived model for the \( P_r \) and \( P_f \).

From (7) and (10), the probability of correct identification and false acceptance over the BSC are computed and receiver operating characteristic (ROC) curves have been shown for different SNRs, database sizes \( M \) and primary list sizes \( N_l \) (Fig. 3 and Fig. 4).
Figure 2. The probability of correct identification and false acceptance of OSLD with $N_l = 8$ over the BSC, where $L = 1024$, $M = 256$ and $\lambda = 0$.

Fig. 3 presents the performance of the OSLD and unique decoder ($N_l = 1$) under various constraints ($\lambda$) on PA. It is confirmed that the privacy improvement comes for the price of a certain performance loss in terms of $P_c$ as a function of $\lambda$. Secondly, the obtained results allow to conclude that the OSLD improves the performance while the probability of correct identification $P_c$ is not close to one.

Fig. 4 shows the impact of $N_l$ and $M$ on the identifier performance. Increasing primary list size $N_l$ improves the identifier performance but after a certain value of $N_l$ it does not change significantly. Finally, increasing database size $M$ decreases the performance.

VII. CONCLUSIONS

In this paper, we investigated the performance of the maximum fixed list size OSLD-based biometric/PUF privacy preserving identification system in terms of the probability of correct identification and false acceptance.

The obtained theoretical and simulation results show that on the one hand, the OSLD can improve the identifier performance in very low SNR scenarios. On the other hand, this improvement is restricted by a certain range of list sizes. Finally, the loss in performance in terms of $P_c$ due to PA is demonstrated for the current system implementation. We are planning to consider the ways of improving the performance/privacy trade-off in our future research.

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