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Modelling the Effect of Electrification on Volcanic Ash Aggregation

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The fine ash released into the atmosphere (particles <63 μm) during explosive volcanic eruptions represents a significant threat for both the ecosystem and many sectors of society. In order to mitigate the associated impact, ash dispersal models need to accurately estimate ash concentration through time and space. Since most fine ash sediments in the form of aggregates, ash dispersal models require a quantitative description of ash aggregation. The physical and chemical processes involved in the collision and sticking of volcanic ash have been extensively studied in the last few decades. Among the different factors affecting volcanic particle aggregation (e.g., turbulence, particle-particle adhesion, presence of liquid and solid water), the charge carried by volcanic particles has been found to play a crucial role. However, Coulomb interactions are not yet taken into account in existing models. In order to fill this gap, we propose a strategy to take charge into account. In particular, we introduce a quantitative model for aggregation of oppositely charged micron—to millimetre-sized objects settling in still air. Our results show that the presence of charge considerably enhances the collision efficiency when one of the colliding objects is very small (<20 μm), and that the sticking efficiency is not affected by particle charge if colliding objects are either small enough (<20 μm) or large enough (>200 μm). Besides providing a theoretical framework to quantify the effect of charge, our findings demonstrate that aggregation models that do not account for electrification significantly underestimate the amount of fine ash that sediments in the form of aggregates, leading to an overestimation of the residence time of fine ash in the atmosphere after explosive volcanic eruptions.

Keywords: volcanic particle aggregation, electrification, collision efficiency, sticking efficiency, collision map

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INTRODUCTION

Volcanic explosive eruptions are typically associated with the injection of a large amount of fine ash (particles <63 μm) into the atmosphere (Rose and Durant (2009)). Recent eruptions have demonstrated the potential threat of volcanic ash on various transport systems (e.g. road network, aviation) as well as agriculture and public health (e.g. 2010 Eyjafjallajökull eruption, Iceland; 2011 Cordon Caulle eruption, Chile; 2020 Taal eruption, Philippines; Lund and Benediktsson (2011); Elissondo et al. (2016)). In order to mitigate the associated risk, atmospheric ash concentration as well as ground mass loading over time and space need to be accurately described. It is important to notice that volcanic ash does not settle as individual particles but is largely affected by size-selective sedimentation processes that include particle aggregation and gravitational instabilities (e.g. Durant (2015)). In particular, extensive field observations show that

during explosive eruptions most of fine ash sediments in the form of aggregates of various types (Taddeucci et al. (2011); Brown et al. (2012); Bagheri et al., 2016). Therefore, a quantitative understanding of aggregation processes is necessary to numerically describe and forecast ash dispersal and sedimentation (e.g. Costa et al. (2010)). Such a quantitative understanding requires the identification and quantification of fundamental parameters that control particle aggregation (e.g. collision velocity, particle mass, particle charge, amount of liquid or solid water on particle surfaces). Among these parameters, charge plays a fundamental role. Volcanic particles are seen to acquire electric charges during magma fragmentation and ejection from the vent (James et al. (2000); Mather and Harrison (2006); Méndez and Dufek (2016)). The spectacular phenomenon of lightning that often takes place during explosive eruptions is the visible proof that electrical potential gradients are present within volcanic plumes (e.g. Cimarelli et al. (2014); James et al. (2008); Cimarelli et al. (2016); Aizawa et al. (2016); Nicoll et al. (2019); Behnke et al. (2018)). The variation of these gradients during ash fall is evidence that volcanic particles are electrically charged. Particle charge can be indirectly estimated by measuring the variation of potential gradients (Hatakeyama (1943); Hatakeyama (1947); Hatakeyama (1949); Hatakeyama and Uchikawa (1951); Hatakeyama (1958)). The first direct measurements of charge carried by settling volcanic particles was performed by Gilbert et al. (1991) at Sakurajima volcano (Japan). Letting volcanic particles fall through the plates of a high voltage condenser, Gilbert et al. (1991) observed that volcanic particles could carry either positive or negative charges the value of which could be close to the ionization limit. They proposed that this charge might arise due to two mechanisms: triboelectric charging and fracture-induced electrification. In particular, the importance of the latter mechanism was stressed during magma fragmentation, suggesting that volcanic particles could preserve a significant charge since their formation. The effectiveness of the fracture-charging mechanism has been experimentally confirmed by James et al. (2000), who measured the charge generated during pumice fracture, obtaining charges of the same order of magnitude as the ones measured by Gilbert et al. (1991). Although volcanic particles seem to be already highly charged at the jet region, their charge can vary during their permanence within the plume and in the atmosphere as a result of several mechanisms. In fact, particles may exchange charge due to triboelectric electrification while colliding. A broad range of experimental evidence exists that triboelectrification (contact electrification) is a size dependent process with small particles preferentially charging negatively and large particles preferentially charging positively (e.g. Lacks and Levandovsky, 2007; Alois et al., 2017). Besides triboelectric charging, particles may undergo other electrification mechanisms: they might break up during collisions acquiring charge due to fractoemission (Mueller et al. (2017)); they may release or adsorb ions contained in the surrounding gas; or they might acquire an induced charge due to the presence of background potentials (Mason (2019)).

Moreover, particle charge distributions vary due to aggregation processes (Dhanorkar and Kamra (1997)), which

in turn are affected by electrical forces. Even though the presence of charge is not required for particles to stick with each other, it has been experimentally shown that Coulomb forces can significantly affect aggregation processes. Experimental evidence of how electrical forces can enhance aggregation was provided by James et al. (1989) who filmed fine charged silicate particles aggregating with each other while settling. Moreover, Schumacher (1994) performed laboratory experiments showing that charged particles settling inside an electric field do aggregate with each other. Therefore, both field observations and laboratory experiments show that electrical forces can strongly affect aggregation processes. However, the magnitude of this impact has not been investigated yet and its effect is not currently taken into account in aggregation models (e.g. Costa et al. (2010)).

The main goal of this study is to quantify the impact that electrical forces can have on aggregation of settling particles. This process is quantitatively described by Smoluchowski (1917), whose population balance equation describes aggregation employing two parameters: the collision kernel and the sticking kernel (Costa et al. (2010); Veitch and Woods (2001)). While the collision kernel is related to the likelihood of particles to collide with each other, the sticking kernel describes the probability that a given collision will end up in sticking (Smoluchowski (1917)). If both these parameters are known at every stage of aggregate growth, the evolution of the grainsize distribution of an aggregate, as well as the total grainsize distribution within a volcanic plume, can be quantitatively characterised. Although the distinction between the collision kernel and the sticking kernel is extremely important for modelling purposes, experimental measurements of those quantities represent a major challenge. For this reason, Gilbert and Lane (1994) measured directly the aggregation coefficient by dividing the number of particles that adhered with each other by the total number of particles.

Experimental measurements for the sticking efficiency were provided by Telling and Dufek (2012). Obtaining collisions between volcanic particles in an enclosed tank, they showed that the sticking efficiency is a decreasing function of the collision kinetic energy, and that relative humidity has a small impact on the sticking behaviour as long as the residence time is low enough. The effect of relative humidity was further investigated by Telling et al. (2013). Their experiments demonstrated that aggregation efficiency was significantly increased for high residence times (>50 min) when relative humidity was higher than 71% due to the development of a water film around the particles. Nonetheless, the expression to compute the sticking based on the experimental investigations of Telling and Dufek (2012) and Telling et al. (2013) is strictly applicable to particles whose diameter is larger than 100 μm , and it is not suitable to investigate the role played by physical parameters such as the object density, object Young's modulus and the object surface energy. Such parameters can change with ash composition, humidity, collision altitude, and they are different for each stage of aggregate growth. Hence, they need to be taken into account by a model that aims to quantify the effect of each variable on aggregation processes. For these reasons, in this study we describe the sticking behaviour employing the

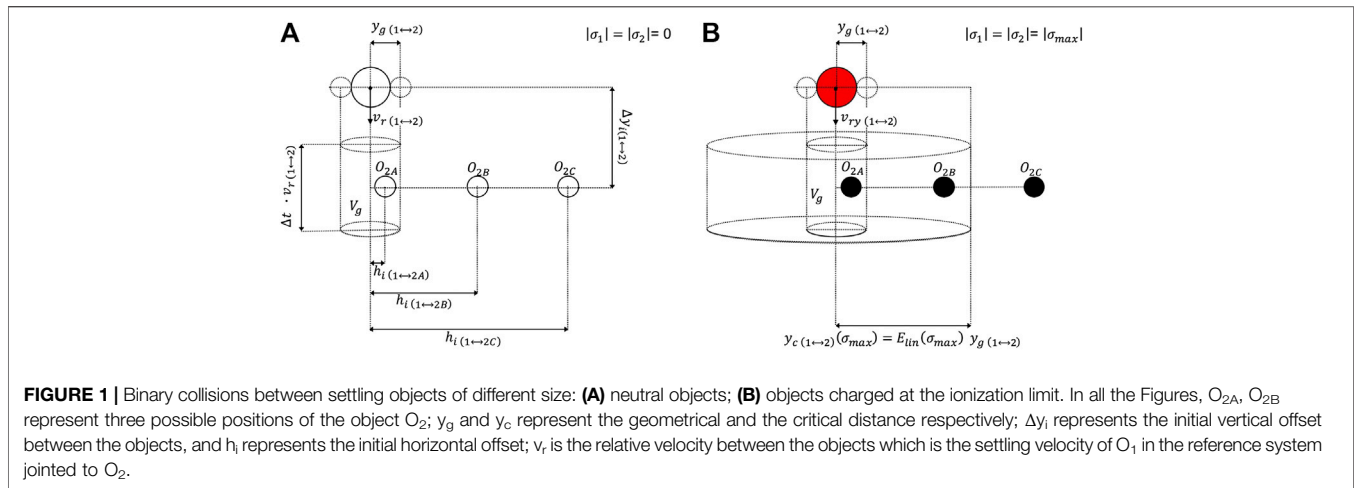


FIGURE 1 | Binary collisions between settling objects of different size: **(A)** neutral objects; **(B)** objects charged at the ionization limit. In all the Figures, O_{2A} , O_{2B} represent three possible positions of the object O_2 ; y_g and y_c represent the geometrical and the critical distance respectively; Δy_i represents the initial vertical offset between the objects, and h_i represents the initial horizontal offset; v_r is the relative velocity between the objects which is the settling velocity of O_1 in the reference system jointed to O_2 .

sticking criterion introduced by Chen et al. (2015), which is based on the theoretical equations derived by Thornton and Ning (1998).

METHODS

In this paper, the effect of charge on both sticking efficiency and collision efficiency is quantified for settling objects, but analysed separately. For objects here we indicate either an individual particle or an aggregate. For the case of an object settling in the atmosphere, the collision kernel with respect to other settling objects can be quantified provided that both the particle/aggregate concentration and the volume swept by the falling object with respect to other objects are known. The concentration of fine ash in the atmosphere can be constrained based on eruptive parameters (e.g. erupted mass and total grain size distribution), on the distance from the vent, and on the collision altitude. In addition, in order to quantify the sticking kernel, we need to know both the kinetic energy of the collision and the mechanical and surface properties of the objects, which determine the ability of the object to dissipate collision kinetic energy.

For simplicity, in this paper we focus on the quantification of the swept volume, which is described by the collision efficiency. The sticking kernel is constrained based on the outcome of every collision. In particular, the relative velocity and the sticking velocity are compared, with the sticking velocity representing the threshold velocity below which two objects stick with each other. This means that in this paper the probability of sticking (i.e. sticking efficiency) is considered to be either 0 (objects rebound) or 1 (objects stick with each other).

In order to compute the sticking efficiency, we will consider the colliding objects to be conductive with zero resistance, in such a way that electrical forces do not play any role after object collision takes place. Although this assumption is strictly valid only when a significant water layer is present on the objects (i.e. $RH > 80\%$), it allows to obtain a conservative estimate on the sticking efficiency. In fact, the assumption implies that objects instantaneously discharge at contact. Hence, in the case of

rebound, colliding objects have no chance of sticking. On the other hand, if objects behave as dielectrics, they might either hold their charge after rebound, or undergo contact electrification during collision. In both cases, they might be able to attract each other again after the first rebound leading to other lower energy collisions that might end up in sticking. These complexities are not considered in this study.

Quantifying the Effect of Coulomb Forces

In order to quantify the effect of Coulomb forces on particle aggregation, we consider a neutral spherical object O_1 settling vertically at its terminal velocity in still air (**Figure 1A**). As mentioned above, this object can represent either an aggregate or a single particle. During its fall, O_1 will eventually reach a slower object O_2 characterised by a lower terminal velocity. As shown in **Figure 1**, the occurrence of the collision between the objects O_1 and O_2 depends on their initial horizontal offset. Objects will eventually collide provided that their horizontal offset is smaller than the geometrical distance y_g , given by the sum of the object radii. The volume V_g swept by O_1 with respect to O_2 during the time interval Δt (**Figure 1A**) is given by:

$$V_g = \pi y_g^2 v_{Ry} \Delta t, \quad (1)$$

where v_{Ry} stands for the vertical component of the relative velocity. Notice that in order for the object O_2 to collide with O_1 during the time interval t , its centre needs to be within the swept volume V_g .

Therefore, the volume swept by an object O_1 with respect to O_2 can be defined as the volume to which the centre of O_2 needs to belong for collision to happen. When the objects O_1 and O_2 are oppositely charged, they will move toward each other horizontally under the effect of Coulomb attraction. As a result, they can collide with each other even if their horizontal offset is higher than the geometrical distance y_g . Therefore, the swept volume is higher for oppositely charged objects compared to neutral objects. Since higher surface charges determine stronger Coulomb forces, the swept volume is an increasing function of surface charges σ_1 , σ_2 .

In order to quantify the effect of charge on collision efficiency, it is useful to consider the maximum volume $V_c(\sigma_{\max})$ that two objects can sweep with respect to each other when they are oppositely charged at the ionization limit (see **Figure 1B**). Hence, when surface charges are between 0 and σ_{\max} , objects will sweep a volume V which is higher than the volume V_g swept by neutral objects, and lower than the maximum volume $V_c(\sigma_{\max})$ swept by fully charged objects.

As shown in **Figure 1B**, both the volumes V_g and $V_c(\sigma_{\max})$ depend on the time interval Δt and on the vertical component relative velocity v_{ry} . Under the assumption that object's charges have a negligible effect on the vertical component of the relative velocity, the heights V_g and $V_c(\sigma_{\max})$ are equal, and the increase in the swept volume only depends on the ratio between the bases of the two cylinders. It is worth noting that this assumption implies that the vertical component of the relative velocity between charged particles is approximated by the corresponding velocity of neutral ones.

This approximation allows us to predict whether two particles will collide or not based on their horizontal offset only.

Objects will eventually collide provided that their horizontal offset is lower than the critical distance y_c . With the term critical distance, we refer here to the critical initial offset y_c beyond which objects will not be able to collide. The existence of this critical horizontal offset was identified by Martin et al. (1979) and employed by Pruppacher and Klett (2010) to take into account the effect of hydrodynamic interactions between objects. Following this approach, we define the electrical collision efficiency as the ratio between the volume swept by relative motion between two oppositely charged objects V with respect to the volume swept by two neutral objects V_g :

$$E_{el} = \frac{V(\sigma_1, \sigma_2, m_1, m_2, \vec{v}_1, \vec{v}_2, A_1, A_2, \mu_f, \rho_f)}{V_g(R_1, R_2)} = \frac{y_c^2}{y_g^2} \quad (2)$$

The symbol $V(\sigma_1, \sigma_2, m_1, m_2, \vec{v}_1, \vec{v}_2, A_1, A_2, \mu_f, \rho_f)$ shows that the actual volume swept by the objects with respect to each other depends on the surface charges σ_1 and σ_2 of the objects, their masses m_1 and m_2 , and on the aerodynamic forces, which depend on the velocity of the objects \vec{v}_1 and \vec{v}_2 , their cross-sectional areas A_1 and A_2 as well as on the density ρ_f and the dynamic viscosity μ_f of the surrounding fluid. The volume V_g swept by neutral objects only depends on the objects' radii.

While the electrical collision efficiency quantifies the increase in the swept volume for charged objects with respect to neutral ones, its square root, which we can call linear collision efficiency, quantifies the increase in the critical distance: $E_{lin} = \sqrt{E_{el}} = y_c/y_g$.

When the electrical collision efficiency is greater than one, electrical forces have the effect of enhancing object collision; conversely, when the linear electrical collision efficiency is lower than 1, electrical forces decrease collisions. These two possibilities correspond respectively to the case of oppositely charged objects ($y_c > y_g$), and the case of like-charged objects ($y_c < y_g$).

In this study, we will focus on the case of oppositely charged objects, which constitute the vast majority of the objects that will eventually collide. In fact, as we will show in the results, the

electrical collision efficiency is always higher than one for oppositely charged objects, and can reach values between 100 and 1,000 for collisions between objects of a few micrometres (as we will show in the result section). Conversely, collision efficiency is always lower than one for likely-charged objects, as the critical distance is lower than the geometrical distance. Therefore, the vast majority of couples of objects that undergo collisions is represented by oppositely-charged objects. This is especially true for micron-sized objects for which the ratio between the collision efficiency for oppositely charged objects and the collision efficiency for likely charged objects can be higher than 1,000. Since micron-sized objects are the ones that are more likely to stick with each other, in this study we focus on collisions between oppositely charged objects only.

The volumetric flow rate of colliding objects is represented by the following equation for the collision kernel K_{el} :

$$K_{el} = \pi y_c^2 v_{ry} = E_{el} \pi y_g^2 v_{ry} \quad (3)$$

In general, the vertical component of the relative velocity v_{ry} is affected by electrical interactions. However, if their effect on the vertical component of the relative velocity is negligible with respect to the settling relative velocity due to the difference in drag, we have $v_{ry} = v_R$.

If we know the linear collision efficiency for a couple of objects, we can multiply it by the geometrical distance and obtain the critical distance. The linear collision efficiency depends on both the size of the considered objects and their surface charge. If the surface charge is a value between zero and the value at the ionization limit, the collision efficiency will be somewhere between the collision efficiency for neutral objects and the collision efficiency for objects charged at the ionization limit. In this study, the linear collision efficiency will be computed for volcanic objects for different size combinations and surface charges.

Neglecting hydrodynamic interactions between the objects and the lift forces, the objects move under the effect of their weight, their mutual Coulomb attraction \vec{F}_{el} , and the drag force \vec{F}_{Drag} . Their motion is therefore described by the following set of differential equations.

$$\begin{cases} \vec{F}_{el\ 2 \rightarrow 1} + \vec{F}_{1\ Drag} + m_1 \vec{g} = m_1 \ddot{\vec{x}}_1, \\ \vec{F}_{el\ 1 \rightarrow 2} + \vec{F}_{2\ Drag} + m_2 \vec{g} = m_2 \ddot{\vec{x}}_2. \end{cases} \quad (4)$$

For a given vertical and horizontal offset between two objects, numerical solution of the system of differential equations can provide the relative position through time, and, therefore, allows us to predict whether the two objects will collide. However, the occurrence of collision is dependent on both the initial vertical offset and the initial horizontal offset between the objects. It is worth noticing here that whatever the vertical offset, two objects of different sizes will eventually reach the same altitude. Therefore, the occurrence of collision will mainly depend on their initial horizontal offset.

In fact, assuming no hydrodynamic interactions, it is reasonable to expect that oppositely charged objects

characterised by different terminal velocities will eventually collide provided that their horizontal offset is small enough, regardless of their starting altitude. Similarly, given the impossibility of carrying an infinite amount of charge, it is reasonable to assume the probability of collision to be zero if their initial horizontal offset is high enough, regardless of their initial vertical offset.

Moreover, for a given charge and a given initial horizontal offset, the lower the relative velocity between the objects, the higher the probability of collision. In fact, when the objects settle at a similar terminal velocity, Coulomb forces have more time at their disposal to accelerate the objects toward each other. Therefore, we estimate the critical horizontal offset by comparing two timescales: the exposure time t_{exp} , and the electrical time t_{el} . While the exposure time represents an estimate for the time that electrical forces have at their disposal to act, the electrical time represents an estimate for the time that electrical forces need to bring the objects to collision. In this framework, the critical distance y_c can be defined as the highest value for which we have $t_{el} < t_{exp}$ (see Appendix B for further details).

Assuming spherical objects characterised by an evenly distributed surface charge, their net charges are $Q_1 = \pi d_1^2 \sigma_1$ and $Q_2 = \pi d_2^2 \sigma_2$. Therefore, the Coulomb interaction they exchange is given by:

$$|\vec{F}_{el}| = \frac{\pi}{4\epsilon_a} \frac{\sigma_g^{-2} d_1^2 d_2^2}{y^2}, \tag{5}$$

where $\epsilon_a = \epsilon_0 \epsilon_r$ is the absolute dielectric constant of the air, $\epsilon_0 = 8.85 \cdot 10^{-12} \text{F/m}$ is the dielectric constant of the vacuum and $\epsilon_r = 1.0006$ is the relative dielectric constant of the air respect to vacuum. In Eq. 5, y represents the distance between the object centres, σ_g is the geometrical mean between the two surface charges, which is given by $\sqrt{|\sigma_1||\sigma_2|}$. The drag forces acting on each object depend on their relative velocities with respect to the air, here considered as a still medium, and cross-sectional areas. They can be computed as follows:

$$\begin{cases} \vec{F}_{1 \text{ Drag}} = -\frac{1}{2} \rho_f A_1 C_{D1} |\vec{v}_1| \cdot \vec{v}_1, \\ \vec{F}_{2 \text{ Drag}} = -\frac{1}{2} \rho_f A_2 C_{D2} |\vec{v}_2| \cdot \vec{v}_2, \end{cases} \tag{6}$$

where \vec{v}_1 and \vec{v}_2 represent the object velocity with respect to the fluid; C_{D1} and C_{D2} represent the drag coefficients of the two objects; A_1 and A_2 represent the cross-sectional areas, and ρ_f represents air density. The cross-sectional areas A_1 and A_2 can be calculated from the object diameters:

$$\begin{cases} A_1 = \frac{\pi d_1^2}{4}, \\ A_2 = \frac{\pi d_2^2}{4}, \end{cases} \tag{7}$$

and the drag coefficients for spherical objects can be obtained with the formula proposed by Clift and Gauvin (1971):

$$C_D = \frac{24}{\text{Re}} \left(1 + 0.15 \text{Re}^{0.687} + \frac{0.42}{1 + (42500/\text{Re}^{1.16})} \right), \tag{8}$$

where the Reynolds number needs to be computed for each object:

$$\begin{cases} \text{Re}_1 = \frac{\rho_f v_1 d_1}{\mu}, \\ \text{Re}_2 = \frac{\rho_f v_2 d_2}{\mu}, \end{cases} \tag{9}$$

Where μ is the dynamic viscosity of the fluid, and ρ_f is the fluid density. Since we are interested in investigating the potential effects of electrical forces on the collision efficiency, it is worth considering the maximum possible charge that an object can carry. This value can be computed from the dielectric strength D_s , which is the electric field above which electrical breakdown occurs. For air, the dielectric strength is approximately 3 MV/m. The electric field generated by a sphere can be calculated with the Gauss theorem. Its value on the sphere's surface is given by:

$$E_{\text{sphere}}(R) = \frac{Q}{4\pi\epsilon_a R^2}, \tag{10}$$

where R represents the radius of the sphere and ϵ_a the relative permittivity of air.

Therefore, the maximum charge that an object can carry in air is given by:

$$Q_{\text{max}}(R) = D_s 4 \pi \epsilon_a R^2. \tag{11}$$

If we assume that the charge is uniformly distributed on the sphere's surface, we can compute the maximum surface charge density:

$$\sigma_{\text{max}} = D_s \epsilon_a. \tag{12}$$

Considering a dielectric strength of 3 MV/m and a relative permittivity of $8.85 \cdot 10^{-12} [\text{C}^2/\text{N m}^2]$, Eq. 12 gives $\sigma_{\text{max}} \approx 27 (\mu\text{C}/\text{m}^2)$.

For every couple of objects, the critical distance was numerically computed finding the maximum initial horizontal offset between the objects for which the collision time was lower than the exposure time. In order to obtain the critical distance, for each couple of sizes, a starting distance equal to 100 times the sum of object radii was considered, and the collision time was computed and compared to the exposure time. The value of the distance was then updated with an iterative procedure based on the bisection method.

Dividing the value of the critical distance by the sum of the object radii, we obtained the linear collision efficiency for different colliding objects. This allowed us to draw collision maps (see following section). When collision occurs, two outcomes are possible: either the objects stick, or they rebound. Sticking will happen provided that the relative velocity v_R is lower than the sticking velocity v_S . Therefore, comparing the relative velocity with the sticking velocity, one can predict the outcome of a collision. The sticking velocity

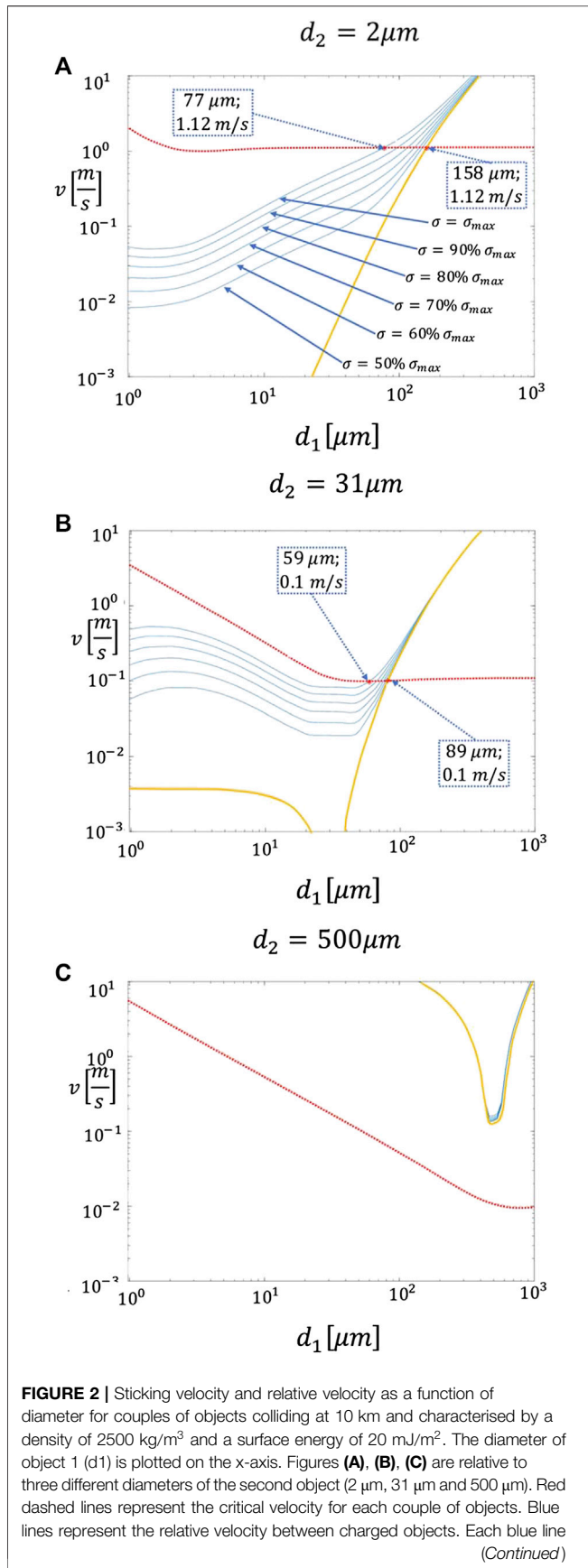


FIGURE 2 | Sticking velocity and relative velocity as a function of diameter for couples of objects colliding at 10 km and characterised by a density of 2500 kg/m³ and a surface energy of 20 mJ/m². The diameter of object 1 (d₁) is plotted on the x-axis. Figures **(A)**, **(B)**, **(C)** are relative to three different diameters of the second object (2 μm, 31 μm and 500 μm). Red dashed lines represent the critical velocity for each couple of objects. Blue lines represent the relative velocity between charged objects. Each blue line (Continued)

depends on the amount of energy that can be dissipated by the forces that act during collision.

The sticking velocity for dry objects can be computed with the formula proposed by Thornton and Ning (1998):

$$V_s = \left(\frac{14.18}{m^*}\right)^{1/2} \left(\frac{\gamma^5 R^{*4}}{E^*}\right)^{1/6}, \quad (13)$$

Where m^* , R^* and E^* represent the reduced quantities for the mass, the radius, and the Young modulus, and γ represents the object surface energy. **Eq. 13** provides the sticking velocity for the interaction between two adhesive spheres. However, it does not take into account for the viscoelastic force that arises during object deformation.

Combining **Eq. 13** with numerical simulations, Chen et al. (2015) obtained an algorithm to compute the sticking velocity which takes also viscoelastic deformation into account. It is worth noting that the values of the sticking velocity computed for viscoelastic particles are higher respect to the ones given in **Eq. 13**. In fact, while **Eq. 13** takes into account for energy dissipation given by adhesive forces, the algorithm proposed by Chen et al. (2015) takes also into account for energy dissipations associated with viscoelastic behaviour of the objects.

In order to obtain upper estimate of the sticking velocity, in this paper we consider the objects to have a viscoelastic behaviour, and therefore we employ the algorithm of Chen et al. (2015) to estimate the sticking velocity. As input parameters, the algorithm of Chen et al. (2015) requires e_0 , which is the restitution coefficient between viscoelastic particles when no adhesive forces are present, and the impact angle. Given the lack of experimental data concerning the restitution coefficient of volcanic particles, the value $e_0 = 0.6$ proposed by Chen et al. was used. Given the impossibility to accurately predict the actual impact angle, a value of zero was considered, which corresponds to head on collisions. Although real collisions between charged settling particles can occur at higher impact angles, the results of Chen et al. show that head on collisions represent a good approximation for impact angles lower than 30°. The Young modulus was set to $E = 142.2$ MPa. This value was computed from the bulk modulus measured for volcanic particles by Ferrari et al. (2013), considering a Poisson’s ratio of 0.21.

It is worth noting that the employed model for computing the sticking velocity is no longer valid if large water layers form around volcanic particles. In fact, if water layers whose thickness is high compared to the surface roughness form around colliding objects, drag forces associated with water layer become the dominant dissipation mechanism. Therefore, the sticking velocity associated with significant water layers is higher than

FIGURE 2 | represents a different value of the surface charge. Surface charges of (50% σ_{max} ; 60% σ_{max} ; 70% σ_{max} ; 80% σ_{max} ; 90% σ_{max} ; 100% σ_{max} are considered). The yellow lines represent the collision velocities between neutral particles. The values for the diameters and of the velocities in the labels are relative to the intersection points between the critical velocity and the relative velocities for both neutral and fully charged objects.

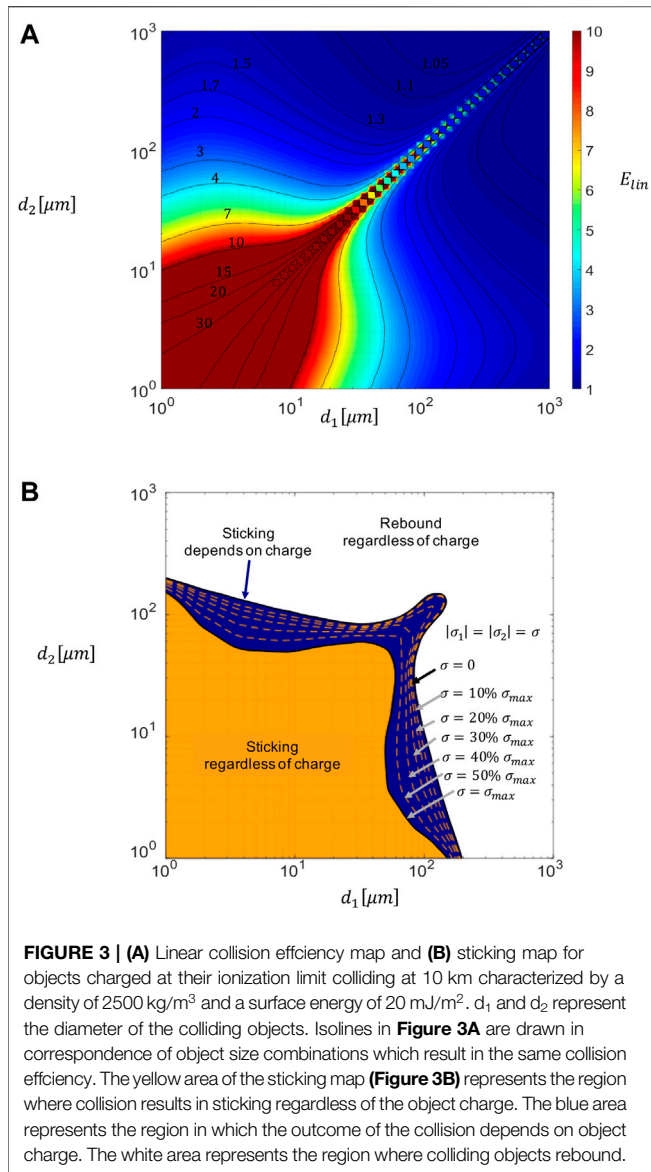


FIGURE 3 | (A) Linear collision efficiency map and **(B)** sticking map for objects charged at their ionization limit colliding at 10 km characterized by a density of 2500 kg/m³ and a surface energy of 20 mJ/m². d_1 and d_2 represent the diameter of the colliding objects. Isolines in **Figure 3A** are drawn in correspondence of object size combinations which result in the same collision efficiency. The yellow area of the sticking map (**Figure 3B**) represents the region where collision results in sticking regardless of the object charge. The blue area represents the region in which the outcome of the collision depends on object charge. The white area represents the region where colliding objects rebound.

the one considered in this work. Moreover, experimental investigations show that electrification is decreased in wet conditions (Stern et al. (2019)).

If the thickness of the water layer is known, the sticking velocity could be computed with the model proposed by Ennis et al. (1991). However, estimation of water layers go beyond the scope of this work.

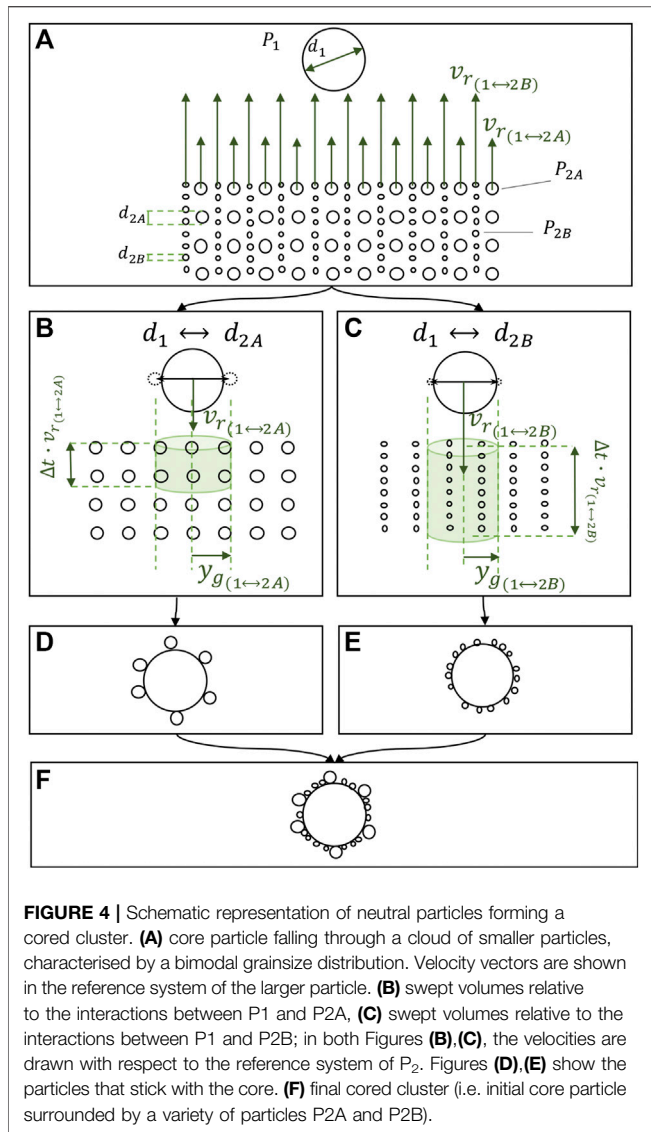
Comparing the sticking velocity with the relative velocity, we obtained the sticking maps, which allow us to identify the size combinations that lead to particle sticking.

RESULTS

The relative velocity and the sticking velocity were computed for many combinations of object diameter D , surface charge σ , density ρ_f , altitude H , and object's surface energy γ . As an

example, in **Figure 2** we show the relative velocity and sticking velocity for couples of objects characterised by the diameters d_1 and d_2 . In order to illustrate the procedure to establish whether colliding objects stick or not, we focus on **Figure 2A**, which is relative to an object characterised by a diameter $d_2 = 2 \mu\text{m}$ colliding with another object whose diameter is the variable d_1 . For neutral objects, the relative velocity is given by the difference between object terminal velocities. The red line represents the sticking velocity for every couple of objects with diameter d_1 and d_2 . The orange line represents the relative velocity that the objects would have if no charge was present on the object's surfaces. In this case the relative velocity would be given by the difference between the object terminal velocities. Blue lines represent the relative velocity between the objects when a charge is present on their surfaces. Different blue lines are relative to different values of the charges present on the object surfaces, which range between 50% of the ionization charge and the ionization charge. All the couples of interacting objects are considered to have the same surface charge and different polarity. Collision velocities between oppositely charged objects are higher than collision velocities between neutral objects because besides having the vertical component given by the difference in terminal velocities, they have a horizontal component which arises due to the fact that objects accelerate toward each other under the effect of Coulomb forces. The horizontal component of the relative velocity depends on both the object charges and the initial horizontal offset between the objects. In fact, provided that objects are close enough to eventually collide, the higher the horizontal offset between them, the higher the horizontal component of the relative velocity at the moment of collision. The maximum horizontal offset that objects can have to eventually collide was defined as the critical distance. The collision velocities for charged objects in **Figure 2** represented by the blue lines were computed assuming that the initial horizontal offset between charged objects is equal to the critical distance each couple of interacting objects. Therefore, blue lines represent the maximum relative velocity between two charged settling objects. In fact, if the initial horizontal offset between the objects is higher than their critical distance, they would not collide. Conversely, if the initial horizontal offset is lower than the critical distance, their relative velocity would be lower than the one represented by the blue lines in **Figure 2**. For example, a 2 μm object will stick with any other object of the same density characterized by a diameter lower than 77 μm (**Figure 2A**). For a 31 μm object, the threshold diameter of the other object decreases to 59 μm (**Figure 2B**). Moreover, if one object is too large, it cannot stick with any other object, regardless of the diameter of the other object (see **Figure 2C**). It is important to note that **Figure 2** was computed for a general density of ash objects (i.e. 2500 kg/m³) as an example. Similar plots can also be compiled for density more suited for aggregates (i.e. <200 kg/m³; e.g. Brown et al. (2012)).

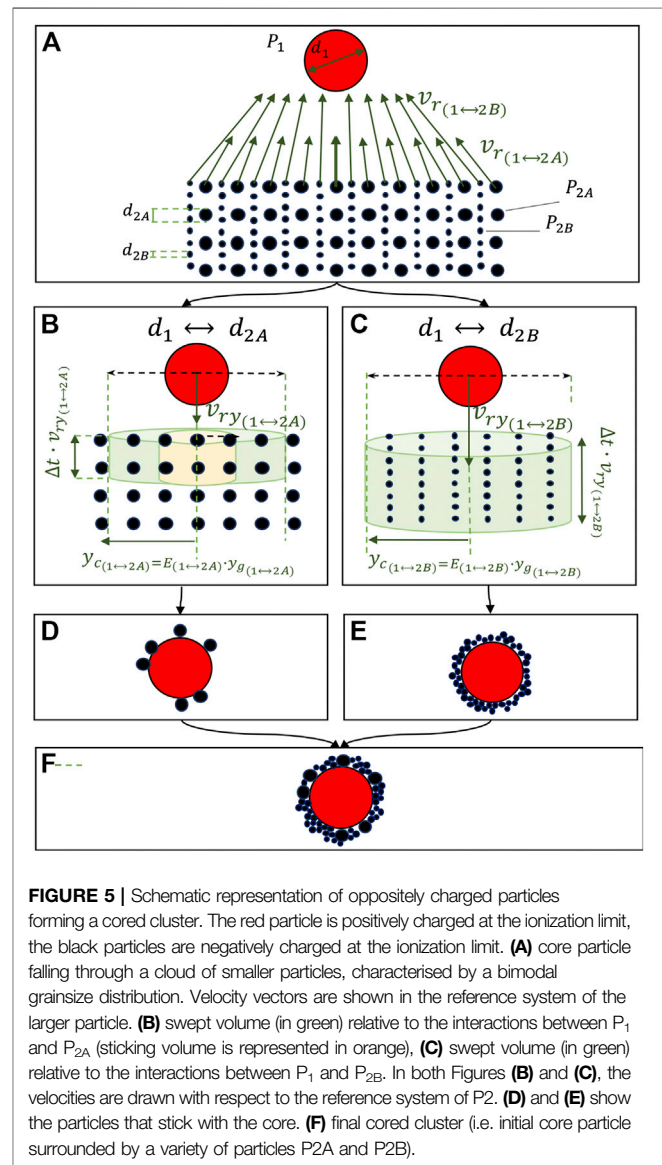
Plots similar to **Figure 2** can be compiled for many other size combinations in order to produce a sticking map and verify whether two objects that collide will also stick. However, prior to a sticking map, we need to compile a collision map to verify whether two objects will collide (e.g. **Figure 3A**). Every point of



the plane in **Figure 3A** corresponds to a couple of interacting objects whose diameters are d_1 and d_2 . Both objects are considered to be oppositely charged at the ionization limit and are characterised by a density of 2500 kg/m^3 (so this specific map is mostly suited to describe collision of ash particles more than aggregates). The collision altitude is set to 10 km. For every point of the plane, the linear collision efficiency was calculated dividing the critical distance by the sum of the radii of the colliding objects. The map shows that the linear collision efficiency increases rapidly for smaller objects (red region), it converges to one for larger objects (blue region) and it is symmetrical with respect to the bisector. Moreover, linear collision efficiency is higher toward the bisector, where the colliding objects are characterised by similar sizes, and, thus, similar terminal velocities. Solutions along this line were not computed: as a matter of fact, such collisions are characterised by a collision efficiency which is either zero or infinite, depending on their initial vertical offset. This is due to the

fact that objects of the same size settle at the same terminal velocity. Therefore, if they are characterised by the same initial altitude, they theoretically have an infinite amount of time to approach each other under the effect of Coulomb attraction, leading to a collision regardless of the initial horizontal offset. On the other hand, if the objects initial altitude is different, they will never collide.

In order to compile sticking maps (**Figure 3B**), plots similar to **Figure 2** were compiled for 100 different size combinations. In the **Supplementary Material**, we also report sticking maps for different values of object densities (ranging between $1,000 \text{ kg/m}^3$ and 2500 kg/m^3); altitude (ranging between 5 and 15 km); and surface energy (ranging between 15 mJ/m^2 and 25 mJ/m^2). **Figure 3B** shows the sticking map for both neutral and charged objects. While **Figure 3A** describes whether two objects collide or not, **Figure 3B** predicts if the two objects stick or not. The diameters d_1 and d_2 of the colliding objects



identify a point on the plot of **Figure 3B**. Since the outcome of the collision between two objects of given sizes depends on their charge, several lines are drawn on the plot. Such lines divide the sticking region by the rebound region and are relative to different values of the object charges. If colliding objects are neutral, the external line is to be considered; if objects are oppositely charged at the ionization limit, the internal line is to be considered. If objects surface charge is a percentage of that at the ionization limit, the corresponding dashed line needs to be considered. Once both the points that correspond to the sizes of the colliding objects and the line that corresponds to object charge are identified, the collision outcome can be predicted by their relative position: if the point is in the internal region delimited by the boundary line, colliding objects will stick; if the point is on the external region, colliding objects will rebound. In order to appreciate the effect of charge on collision outcome, it is worth noticing that the boundary lines divide the quadrant in three regions. One in which colliding objects will always rebound regardless their charge (white region); one in which objects will always stick regardless of their charge (orange region), and one in which the collision outcome depends on the charge (blue region).

Since every aggregate is the result of a series of binary collisions between objects that ended up in sticking, its evolution can be described provided that the occurrence and the outcome of every collision can be predicted. A collision map (e.g. **Figure 3A**) can be compiled based on the density of the colliding objects, the magnitude of their surface charges and the altitude at which collision happens. Nonetheless, in order to compile a sticking map (i.e. **Figure 3B**), the surface energy of the object also needs to be known. In particular, if both the initial horizontal offset between the objects are known, **Figures 3A,B** can be used to determine whether the objects will collide, and to predict whether they will stick. While the collisions occurrence can be determined with **Figure 3A**, the collision outcome (sticking or rebound) can be determined with **Figure 3B**.

The formation of an aggregate is characterised by a succession of several collisions that end up in sticking. In order to illustrate how collision and sticking maps can be used to describe aggregate evolution in the case of a cored cluster (an aggregate formed by a larger particle in the middle surrounded by a crust of finer particles), we consider the simple case of a core object (i.e. individual particle) falling through a homogeneous cloud of smaller particles characterised by a bimodal grain size distribution (**Figure 4**). If the real grain size distribution is known, the same reasoning can be repeated for all the possible size combinations. Let the core's diameter be $d_1 = 70 \mu\text{m}$. And let the diameters of the other particles be $d_{2A} = 15 \mu\text{m}$ and $d_{2B} = 1 \mu\text{m}$. In **Figure 4A**, particle velocities are shown in the reference system joint to the core. The relative velocity is higher for smaller particles as their terminal velocity is much lower than the core velocity. In order to predict the occurrence and outcome of core-particle collisions, it is convenient to consider separately the interaction between particles of different sizes. In **Figure 4B**, the interaction between the core and $15 \mu\text{m}$ particles is considered. The green volume represents the volume swept by the core respect to the particles P_{2A} . The volume swept per unit time is proportional to the

relative velocity, which can be read from **Figure 4**: $v_{R(1-2A)} = 0.35 \text{ m/s}$. The radius of the base is given by the geometrical distance $y_g = 42.5 \mu\text{m}$. The volume swept in one second is $V_{s(1-2A)} = 1.98 \text{ mm}^3$. Similarly, **Figure 4C** represents the interaction between P_1 and P_{2B} . The relative velocity is $v_{R(1-2B)} = 0.40 \text{ m/s}$, the geometrical distance is $y_g = 35.5 \mu\text{m}$, and the swept volume in 1 s is $V_{s(1-2A)} = 1.58 \text{ mm}^3$. Multiplying the particle concentration in mass by the swept volume, one can get the mass of particles that will collide with the core. Identifying the points that identify the collision on **Figure 3B**, one can predict that both the particles P_{2A} and P_{2B} will stick to the core P_1 . Therefore, all the colliding particles will stick to the core as shown in **Figures 4D,E**. Combining 4D and 4E, we get all the particles that will stick to the cored cluster. Note that the geometry of the aggregate is not taken into account in the model, which is only able to tell the final grain size distribution of the aggregate as a function of particle concentration.

Let us now consider the same case for charged particles sketched in **Figure 5**. In this case, a horizontal component of the relative velocity will arise due to electrical attraction, as shown in **Figure 5**. However, the effect of the horizontal component on the relative velocity, is already taken into account behind the computation of the collision and sticking maps. For this reason in **Figures 5B,C** we only consider the vertical component of the relative velocity, which is given by the difference between the terminal velocities.

In **Figure 5B** two volumes are identified. The green one represents the collision volume inside which particles will collide. Comparing **Figure 5B** with **Figure 4B** one can appreciate the increase in the collision volume for charged particles with respect to neutral particles. However, out of all the particles that will eventually collide only the ones inside the yellow volume will end up in sticking. In fact, particles that are inside the green volume and outside the yellow volume have more room to accelerate under the effect of Coulomb interaction. For this reason, they collide at a velocity that is too high for sticking to happen. The radius of the green volume corresponds to the critical distance, which can be calculated from the linear collision efficiency given by **Figure 3A**. The radius of the yellow volume is the sticking distance, which we define has the horizontal offset below which particles will eventually collide and stick.

Linear collision efficiency for the interaction between the core and $15 \mu\text{m}$ particles is $E_{(1-2A)} = 2.5$. For the interaction between the core and the $1 \mu\text{m}$ particles, it is $E_{(1-2B)} = 3.4$. The increase in the swept volume for the particles charged at the ionization limit with respect to the neutral case is given by **Eq. 2**. Substituting the numbers, we obtain that the volume increases 6.25 times for the interaction between the core and $15 \mu\text{m}$ particles, and it increases 11.56 times for the interaction between the core and $3 \mu\text{m}$ particles. Finding the points that correspond to particle diameters on **Figure 3B**, we see that the core will always stick with $1 \mu\text{m}$ particles.

DISCUSSION

Our analysis shows that both the collision efficiency and the sticking efficiency of settling objects can be predicted

computing collision maps and sticking maps (e.g. **Figures 3A,B**). Although both maps are computed for a given collision altitude (10 km), a given object density (2500 kg/m³), and the sticking map is drawn for given surface tension (20 mJ/m²), their shape allow to draw some general qualitative conclusions about aggregation of settling volcanic particles and aggregates.

Numerical Simulations vs Analytical Solutions

Although charge dependent approximated formulas could be theoretically derived for both collision efficiency and sticking efficiency, the presence of velocity dependent drag forces (Eq. 6) for a wide range of Reynolds numbers (Eq. 9) makes it impossible to find an analytical closed form solutions. For this reason, we opted for numerical simulations. Even in the case in which drag forces can be considered negligible with respect to electrical forces, analytical solutions for the collision efficiency are rather challenging, but not impossible. In fact, the motion of two objects in an inverse-square field is known in classical mechanics as the two-body problem, which has analytical solutions. Although a complete theoretical solution is beyond the scope of this paper, in **Appendix A, B** we lay out the foundation for such a derivation. Moreover, in the **Supplementary Material** we employ an analytical expression for the collision velocity to derive equations to apply the sticking maps to objects released at an arbitrary initial offset.

Increase in Collision Frequency: Impact of Object Charge and Size

The collision map (**Figure 3A**) shows that the collision efficiency is dramatically enhanced for small objects (<10 μm) charged at the ionization limit. This is mainly due to their low inertia, which allows Coulomb forces to effectively accelerate the objects toward each other. Moreover, the enhancement effect of Coulomb forces is more important when the oppositely charged objects have similar sizes. This is due to the fact that objects characterised by similar sizes also have similar terminal velocities, and, therefore, a lower relative velocity. As a result, they stay close to each other for long enough for the electrical forces to act. However, it is worth noting that objects of similar size that have undergone triboelectric charging are likely to carry charges of the same polarity (Lacks and Levandovsky (2007)). Therefore, despite the fact that the highest enhancement of collision efficiency is theoretically obtained for two small (<10 μm) oppositely charged objects of similar size, in reality the highest enhancement may be reached when just one of the colliding objects is small (<10 μm).

In fact, numerous experimental studies have indicated that contact electrification/triboelectrification preferentially charges small objects negatively and large objects positively as a consequence of collision (e.g. Lacks and Levandovsky, 2007; Alois et al., 2017). Such a size dependence in polarity would enhance the creation of aggregates due to attraction of small

(negative) objects to large (positive) objects compared to the case where there is no size dependence.

The effect of object size on collision can be seen comparing **Figures 4B,C**. When the collected object is small (**Figure 4C**), the volume swept per unit time stretches vertically due to the higher relative velocity and shrinks laterally due to the smaller geometrical distance. The second effect is dominant with respect to the first one. Opposite charge has the effect of dramatically increasing the swept volume. As can be seen comparing **Figure 5B** with **Figure 4B**, and **Figure 5C** with **Figure 4C**, the volume increase is more important when the collected object is small. The result is that small objects will collide more than large objects, despite the lower geometrical distance.

Reduction of Sticking Efficiency: Impact of Object Charge, Size, Density, Surface Energy and Collision Altitude

Figure 3B shows that collision between small objects (i.e. all the size combinations relative to the golden area of **Figure 3B**) end up in sticking regardless of their charge. This happens because their mass is low enough for the collision kinetic energy to be dissipated. On the other hand, collisions between the objects characterised by the size combinations in the blue area of **Figure 3B** stick to each other only if the colliding objects are neutral. This happens due to their low collision velocity, which keeps the collision kinetic energy lower than the threshold value for sticking. This study shows that on one hand the presence of an opposite charge on objects always determines more collisions compared to neutral objects (see **Figure 3A**, where the linear collision efficiency is always greater than 1), and on the other hand it decreases the sticking efficiency for big objects. Moreover, depending on object size, charged objects might not stick with each other even when their neutral counterparts would stick (**Figure 5B**). This is caused by the increase in relative velocity that occurs just before collision due to Coulomb interactions. However, this result is based on the assumption that electrical forces do not affect the sticking velocity between objects. The lower sticking region of charged objects can be quantitatively described by the 'sticking volume' shown in **Figure 5B**, which is smaller than the swept volume. The combination of the effects of charge on sticking and collision ultimately lead to a finer grain-size distribution for charged aggregates (**Figures 4F, 5F**). This occurs not only due to the significant increase in the collected smaller particles, but also as a result of a higher number of larger particles that collide and rebound.

Since the sticking behaviour of objects is strongly dependent on their density, in **Appendix C** we show how these parameters affect the sticking maps. Results allow to quantitatively explain some known facts about volcanic particle aggregation. Firstly, the higher the surface energies, the bigger the size of the objects that can stick (**Figure 3C**; Appendix C). This explains why wet aggregates, which are characterised by high surface energies, contain large particles (i.e. coarse ash). Secondly when collisions happen at lower altitudes, larger particles can stick (**Figure 2C**; Appendix C). This happens because if objects collide at low altitudes, their relative velocity is lower due to

the higher density of the surrounding fluid. The implication of this is that the altitude at which aggregates form has an effect on the internal grain-size distribution. Finally, when the colliding objects have lower densities, larger particles can stick (**Figure 1C**; Appendix C). This is one of the reasons why for the same given size two aggregates are more likely to stick than two particles.

In conclusion, besides providing a quantification of the effect of charge, the obtained collision and sticking maps represent a powerful tool to quantitatively describe the effect that all the possible parameters can have on aggregation of volcanic particles and aggregates.

Collision and Sticking Maps: Limits of Applicability

The model proposed in this paper describes collisions between dry objects, which take place during particle sedimentation in still air. However, the maps (**Figures 3A,B**) provide meaningful constraints also when the conditions mentioned above are not fully satisfied. In order to clarify these constraints, we review and discuss each assumption behind the model.

The “still air” assumption (i.e. no wind and no turbulence) allowed us to compute the relative velocities between the objects considering only the combined effect of differential settling, Coulomb forces and drag forces. When the effect of wind and turbulence are not negligible, the relative velocities between the colliding objects may be higher with respect to the ones predicted in our model. As a result, wind and turbulence may increase the collision efficiency and decrease the sticking efficiency. Therefore, when the “still air” assumption is not verified the collision map (**Figure 3A**) may provide a lower bound to the collision efficiency, and the sticking map (**Figure 3B**) may provide an upper bound to the sticking efficiency.

Since Brownian motion and fluid shear were not considered in the model, the maps are applicable to size combinations for which differential settling is the dominant collision mechanisms. This is true provided that the smallest object is larger than 1 μm and the largest one is larger than 4 μm . In fact, the comparison between the order of magnitudes of different collision kernels provided by Costa et al. (2010) shows that for the sizes mentioned above, the collision kernel associated with differential settling is at least one order of magnitude higher than the one associated with Brownian motion, and at least five orders of magnitude higher than the one associated with fluid shear. Moreover, when the diameter of the large object is larger than 10 μm , the collision kernel associated with differential settling is at least two orders of magnitude higher than the one associated with Brownian motion.

Since our model focuses on dry aggregation, it can be directly applied provided that the relative humidity of the surrounding environment is lower than 71%. In fact, according to Telling et al. (2013) this is the threshold value beyond which water films start to form on the objects. If the mass of the water layers is negligible with respect to the mass of the particles, the collision map is still applicable. Regarding the sticking map (**Figure 3B**), it can still be applied to obtain a conservative

estimation of the sticking efficiency as wet objects stick more easily than dry objects.

Since spherical objects of the same density are characterised by the same settling velocity, our model is not applicable to collisions between objects of similar size. In fact, the maps (**Figures 3A,B**) were obtained considering only couples of objects such that the largest one is at least 10% larger than the smallest one. Therefore, the points around the bisector should not be considered when applying either map (**Figures 3A,B**).

It is worth reminding here that the collision map (**Figure 3A**) and the sticking map (**Figure 3B**) were obtained considering that both the objects are colliding at an altitude of 10 km above sea level, they are characterised by a density of 2500 (kg/m^3), a Young modulus of 142.2 MPa, and a surface energy of 20 (mJ/m^2). As the parameters describing the objects change, the maps change accordingly. In the **Supplementary Material**, we show and discuss in detail how the sticking map changes with varying object density, collision altitude and object surface energy.

Furthermore, when applying our model to real particles, we need to take into consideration the fact that their charge might exceed the maximum surface charge, and we need to be aware of the implications of an irregular shape. These effects are discussed below for both the collision and the sticking maps. Regarding the collision map (**Figure 3A**), it is directly applicable when the colliding objects are oppositely charged with surface charges of $|\sigma_1| = |\sigma_2| = \sigma_{\text{max}} = 27 (\mu\text{C}/\text{m}^2)$. Although this value is commonly considered to be the maximum surface charge that spherical particles can have in standard atmosphere, experimental investigations show that fine particles ($<10 \mu\text{m}$) can carry higher surface charges (Hamamoto and Nakajima, 1992). Therefore, the enhancement of collision efficiency for fine particles can be even higher than the one shown in **Figure 3A**.

Moreover, since irregular objects will have in general higher drag forces than spherical ones (Bagheri and Bonadonna, 2016), the values given in **Figure 3A** constitute an upper limit for the linear collision efficiency of real objects. Regarding the sticking map, the fact that fine particles can carry surface charges that are higher than 27 $\mu\text{C}/\text{m}^2$ has no significant effect on the applicability of **Figure 3B** due to the fact that fine particles stick regardless of their charge. Since irregular particles reach lower collision velocities respect to spherical objects (due to higher drag forces), the sticking areas for irregular particles are larger than the ones shown in **Figure 3B**. In order to show in depth how the maps can be applied to specific objects with specific charges, in the **Supplementary Material** we provide flowcharts with all the possible cases.

Since our model considers differential settling to be the dominant collision mechanism, the provided maps cannot be directly applied inside the volcanic plume, where turbulence plays an important role. Computation of collision and sticking maps inside the plume requires the knowledge of relative velocity for all the size combinations. Since these velocities strongly depend on the eruption parameters, it is not possible to obtain maps of general validity.

However, the qualitative results regarding the effect of oppositely charged objects with respect to neutral ones might still hold within the volcanic plumes and clouds. In fact, all the other parameters

TABLE 1 | total grain size distribution associated with the eruption of Eyjafjallajökull (2010) between 5–8 May 2010, (Bonadonna et al. (2011))

Diameter (micron)	Cumulative mass fraction
1	0.006
3	0.056
10	0.256
30	0.956
100	1

being equal, oppositely charged objects will always lead to an increase in the swept volume, and an increase in the relative velocity with respect to neutral objects and similarly charged objects. Therefore, we expect that charged objects lead to the formation of aggregates which are richer in fine ash regardless of the environment where they form (plume, cloud, or atmosphere).

Field Observations of Oppositely Charged Objects and Aggregate Grain Size that Support the Proposed Model

The conclusion that charged objects form aggregates which are richer in fine ash has general validity provided that oppositely charged objects are present in the volcanic plume and cloud, and that most collisions occur between oppositely charged objects. The presence of oppositely charged particles is confirmed by the field observations performed by Miura et al. (2002), which show that the charging mechanism seems to be size dependent, leading to scenarios such as the one sketched in Figure 1B. The fact that most collisions occur between oppositely charged particles is a consequence of the fact that couples of particles carrying the same charge sweep a smaller volume than both neutral and oppositely charged particles.

In order to show how our model can be applied to a volcanic context, we reviewed several grain-size distributions available in literature. To date, grain-size distributions have been determined for

all aggregate types (e.g. Bagheri et al. (2016); Bonadonna et al. (2002); Bonadonna et al. (2011); Brazier et al. (1982); Burns et al. (2017); van Eaton and Wilson (2013)). In particular, Bagheri et al. (2016) presented the grain-size distribution of cored clusters formed at Sakurajima volcano. As an example, we consider one of the aggregates they identified which was composed of a 250 μm core, and a shell which included particles between 8 and 44 μm . If both the particle surface energy and the colliding altitude were known, a sticking map could be compiled in order to see whether the grain-size distribution is compatible with the scenario of an aggregate formed during settling. Assuming the conditions of Figure 3B (i.e. a surface energy for dry particles of 20 mJ/m^2 , which is the value for silica, and a particle density of 2500 kg/m^3 , which is the mean particle density measured by Bagheri et al. (2016)) a 250 μm particle would not be able to stick with any other particle. Therefore, aggregate formation must have started in an environment where particles had either a higher surface energy, maybe due to high humidity, or lower relative velocity. It is likely that the 250 μm particle has found such conditions in the higher portion of the plume, where the plume mixture might have reached the saturation point, and water layers might have formed around the particles, determining a high surface energy. Indeed, by measuring the settling time of aggregates, Bagheri et al. (2016) also estimated that aggregates were likely to be formed in the higher part of the plume.

Collision Frequency: The Impact of Particle Concentration

The map in Figure 3A provides the normalised critical distance, which is the ratio between the critical distance and the sum of the radii of colliding particles. The electrical collision efficiency, which quantifies the enhancement of the swept volume due to Coulomb interactions, can be obtained by computing the square of the normalised critical distance. For example, a normalised critical distance of 30 implies that charged objects sweep an effective volume that is 900 times larger than the volume swept by

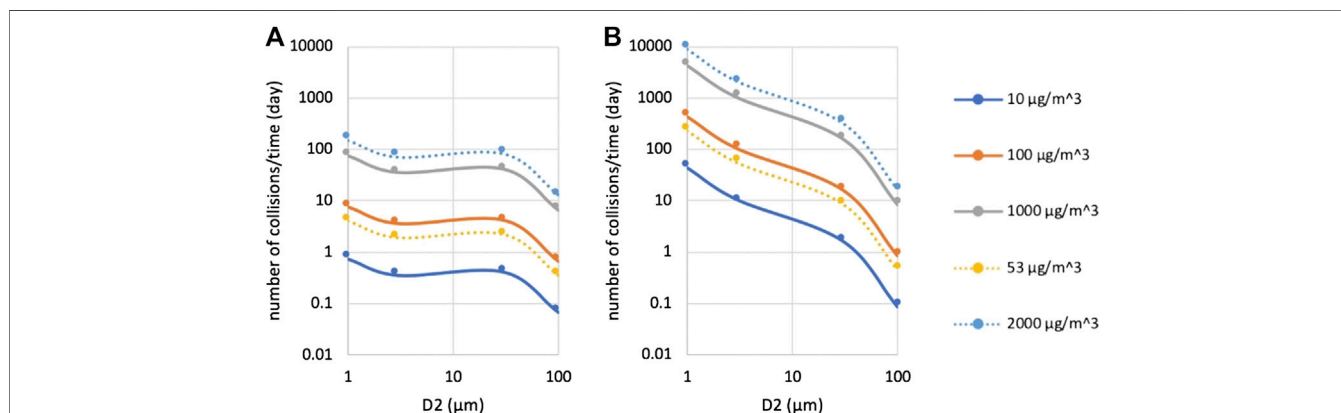


FIGURE 6 | Collision rate with respect to one specific particle whose diameter is $D_1 = 10 \mu\text{m}$, interacting with another particle whose diameter is represented by D_2 . Different lines correspond to different concentration values. While solid lines show three different orders of magnitudes (10 $\mu\text{g}/\text{m}^3$, 100 $\mu\text{g}/\text{m}^3$, 1,000 $\mu\text{g}/\text{m}^3$); dashed lines are relative to the values measured by Weber et al. (2012) in May 2010 at Eyjafjallajökull (Iceland) (see text for details). (A) is relative to neutral particles; (B) is relative to oppositely charged particles at the ionization limit.

neutral particles. In addition, the collision kernel can be computed by multiplying the collision efficiency by the geometrically swept area and the relative velocity in order to constrain the volumetric flow rate of colliding particles (Eq. 3). As discussed in previous sections, aggregation of volcanic particles strongly depends on both collision efficiency and sticking efficiency. In particular, collision rate with respect to any particular object (i.e. amount of collisions per unit time) depends on particle number concentration n (i.e. number of particles per unit volume):

$$\frac{\# \text{collisions}}{\text{time}} = n K_{el} = n E_{el} \pi r_g^2 v_{Ry}, \quad (14)$$

If both the mass concentration and the mass fractions are known, the particle number concentrations can be computed for every size combination. The concentration of particles associated with volcanic eruptions depends on several factors such as the eruption physical parameters, the meteorological conditions, the altitude of the plume/cloud and the distance from the vent. An example of how particle concentration changes with altitude is provided by Moxnes et al. (2014), who report measurements of ash concentration over Stockholm after the 2011 Grimsvötn eruption (Iceland). Their profiles show that mass concentration varies between 0 and 300 $\mu\text{g}/\text{m}^3$ for altitudes between 0 and 4 km.

In-situ investigations carried out between 9 and 11 May 2010 during the eruption of Eyjafjallajökull (Iceland) showed that ash concentration at 45–60 km from the vent was below 53 $\mu\text{g}/\text{m}^3$ outside the plume and could reach 2000 $\mu\text{g}/\text{m}^3$ at the outskirts of the volcanic cloud (Weber et al. (2012)).

In order to show the effect of electrical forces on collision rate, we calculated the particle number concentration associated with different particle size employing the grain-size distribution derived from both field and remote-sensing information (Table 1), and assuming spherical particles with a density of 2500 kg/m^3 . We computed the number of collisions per day for a 10 μm particle interacting with other particles between 1 and 100 μm (Figures 6A,B). Computations were done for three order of magnitudes of concentrations (10 $\mu\text{g}/\text{m}^3$, 100 $\mu\text{g}/\text{m}^3$, 1,000 $\mu\text{g}/\text{m}^3$), and for the concentrations measured by Weber et al. (2012) at Eyjafjallajökull (53 $\mu\text{g}/\text{m}^3$, 2000 $\mu\text{g}/\text{m}^3$). The enhancement in the collision rate due to electrical forces is clearly more important for fine particles (Figure 6).

CONCLUSIONS

Numerical simulations have been performed to study the effect of charge on aggregation of settling ash in still air. Since an aggregate is formed as a result of a series of binary collisions, we considered the interactions between couples of objects (i.e. either particles or aggregates). For a given altitude, object density and surface energy, a collision map (Figure 3A) and a sticking map (Figure 3B) were obtained to predict whether a couple of objects will collide and stick with each other.

The collision map (e.g. Figure 3A) shows that oppositely charged objects are more likely to collide than neutral ones as they sweep a larger volume. In particular, the increase in swept

volume is progressively more important for smaller objects of similar sizes. However, since objects of similar size are likely to carry charges of the same polarity due to the nature of triboelectric charging, the couples of objects that benefit the most from an electrically driven enhancement in collision efficiency are the ones that involve one small object (<10 μm) and a larger object of the opposite polarity. This combination is likely to happen for every collision that contributes to the formation of an aggregate. In this case the larger object is represented by the aggregate itself and the smaller object is represented by the particle that is being aggregated.

Moreover, the sticking map (e.g. Figure 3B) allows to determine the collision outcome for both neutral and oppositely charged colliding objects. In particular, it shows that if colliding objects are small enough (<20 μm) they will stick, and if they are large enough (>200 μm) they will rebound regardless of their charge. However, there is a transition region in which the collision outcome depends on surface charge, with highly charged particles being more likely to rebound due to their higher collision velocity. Therefore, not taking charge into account leads to an overestimation of the number of objects between 20 and 200 μm that stick with each other.

Given that aggregates form as a result of a series of binary collisions that end up in sticking, the combined use of collision and sticking maps allows to quantify the effect of charge on grain size distribution. Since the enhancement in collision efficiency is more important when one of the colliding object is small (<10 μm), aggregates that are composed by charged particles are expected to contain more fine ash than aggregates composed by neutral particles (Figures 4, 5). Therefore, aggregation models that do not take charge into account significantly underestimate the amount of fine ash that sediments in the form of aggregates.

If both particle concentration and grain-size distribution in the atmosphere are known, the collision map can be used to estimate the number of collisions per unit time that a particular object experiences. Such a number was computed for the 2010 eruption of Eyjafjallajökull under the assumption of constant ash concentration in the atmosphere (See Figures 6A,B). Considering the interaction between a 1 μm and a 10 μm object as an example, we showed that neglecting the effect of charge leads to underestimating by almost three orders of magnitude the number of collisions.

Even though our analysis focuses on aggregation of objects settling in still air, the same framework can be extended in future studies to study aggregation in the volcanic plume and cloud, where the combined effect of Coulomb forces and turbulent forces needs to be considered. Although more experimental investigations are needed to establish the exact values of both the collision efficiency and the threshold sizes for sticking of volcanic objects, our study provides a way to quantify the magnitude of the effects of charge on aggregation processes, which should be taken into account in future aggregation models.

Although electric charge affects both collision and sticking efficiency (as shown in Figures 3A,B), considering even only the effect of charge on collision efficiency would be enough to

considerably improve the estimates of fine ash concentration in the atmosphere. In fact, neglecting object charge leads to a significant overestimation of the amount of fine ash that remains airborne. Since accurate estimations of fine ash concentration in the atmosphere are necessary to mitigate volcanic risk, it is of primary importance that aggregation models take at least the effects of electrification on collision efficiency into account.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/**Supplementary Material**, further inquiries can be directed to the corresponding author.

AUTHOR CONTRIBUTIONS

SP conducted this work as part of his Ph.D. He developed the theoretical framework and performed the numerical simulations under the supervision of CB and ER. JM largely contributed to the

interpretation of the results. All authors were involved in the finalization of the manuscript.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/feart.2020.574106/full#supplementary-material>.

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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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