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ARTICLE OPEN

Nodeless superconductivity and its evolution with pressure in the layered dirac semimetal 2M-WS₂Zurab Guguchia¹, Dariusz J. Gawryluk², Marta Brzezinska^{3,4}, Stepan S. Tsirkin³, Rustem Khasanov¹, Ekaterina Pomjakushina², Fabian O. von Rohr^{3,5}, Joel A. T. Verezhak¹, M. Zahid Hasan⁶, Titus Neupert³, Hubertus Luetkens¹ and Alex Amato¹

Recently, the transition metal dichalcogenide (TMD) system 2M-WS₂ has been identified as a Dirac semimetal exhibiting both superconductivity with the highest $T_c \sim 8.5$ K among all the TMD materials and topological surface states. Here we report on muon spin rotation (μ SR) and density functional theory studies of microscopic SC properties and the electronic structure in 2M-WS₂ at ambient and under hydrostatic pressures ($p_{\max} = 1.9$ GPa). The SC order parameter in 2M-WS₂ is determined to have single-gap s -wave symmetry. We further show a strong negative pressure effect on T_c and on the SC gap Δ . This may be partly caused by the pressure induced reduction of the size of the electron pocket around the Γ -point. We also find that the superfluid density n_s is weakly affected by pressure. The absence of a strong pressure effect on n_s and the absence of a correlation between n_s and T_c in 2M-WS₂, in contrast to the other SC TMDs T_d -MoTe₂ and 2H-NbSe₂, is explained in terms of its location in the optimal (ambient pressure) and above the optimal (under pressure) superconducting regions of the phase diagram and its large distance to the other possible competing or cooperating orders.

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INTRODUCTION

The transition metal dichalcogenides (TMDs) are representative layered materials presently attracting very strong interest from research communities working on nanoscience and 2-d layered systems.^{1–14} The TMDs share the MX₂ chemical formula, with M being a transition metal (M = Ti, Zr, Hf, V, Nb, Ta, Mo, W or Re) and X being a chalcogen (X = S, Se, or Te). TMDs are obtained in various crystal structures 1T, 2H, and 1T' with different stackings of the individual MX₂ layers. A number of ground states have been observed in these systems including charge-density waves, superconductivity, semiconductors and topological metals. New physics findings in TMDs include strong excitonic states, novel phenomena from valley splitting, Dirac cone dispersion and topological effects, and more.^{1,4}

Layered materials, with highly anisotropic electronic properties have been found to be potential hosts for unconventional superconductivity. TMDs exhibit many features strikingly similar to those reported in other unconventional superconductors. Superconductivity can be observed under pressure as for the pristine 1T polytype TMD materials which are not superconducting at ambient pressure, but exhibit charge density wave (CDW) states, instead.¹⁵ The metallic 2H polytypes have two, or more, Fermi surfaces and saddle bands, allowing for dual orderings, which can be coexisting CDW and SC orderings, two superconducting gaps, two CDW gaps, and possibly even pseudogaps above the onset temperature of CDW orderings, as reported in some cuprate superconductors.^{16–18} Upon application of pressure, the CDW ground state is suppressed and the superconducting transition temperature is enhanced. A dome-like superconducting

phase was induced by electrostatic gating in the semiconducting 2H-MoSe₂, 2H-MoS₂, 2H-MoTe₂, and 2H-WS₂ with a T_c of up to 10 K.^{19–21} It was also shown that using field effect gating, one can induce superconductivity in monolayer semiconducting TMD WS₂,²² and one could access an unprecedented doping range revealing a rich set of competing electronic phases ranging from band insulator, via superconductor, to a reentrant insulator at high doping. Superconductivity with a very low $T_c \sim 0.1$ K was also reported in the Weyl semimetal MoTe₂ which exhibits a low temperature orthorhombic T_d structure.⁵ However, under the application of pressure, the orthorhombic structure transforms into the 1T' structure and T_c is enhanced to about 8 K. Recently, we found a correlation between the superfluid density at $T = 0$ and the transition temperature T_c in the type-II Weyl semimetal T_d -MoTe₂,²³ and the deviation from the linear correlation in 2H-NbSe₂ under pressure.²⁴ These observations resemble the ones found earlier in cuprates^{25–30} and Fe-based superconductors.^{31–34} These examples demonstrate that the TMDs exhibit rather unconventional superconducting and normal state properties.

Recently, superconductivity with $T_c \sim 8.8$ K was reported in the new compound 2M-WS₂, which is constructed from 1T'-WS₂ monolayers.³⁵ 2M-WS₂ has the highest T_c among all TMD materials at ambient pressure. The system possesses a semimetallic band structure. The crystal structure of 2M-WS₂ has a different stacking of 1T'-WS₂ monolayers along the a -axis, compared to T_d -MoTe₂ and 1T'-WTe₂. In addition to superconductivity, topological surface states with a single Dirac cone were theoretically predicted for 2M-WS₂. Hence, this system represents one of the few examples of a material with both superconductivity and a topologically non-

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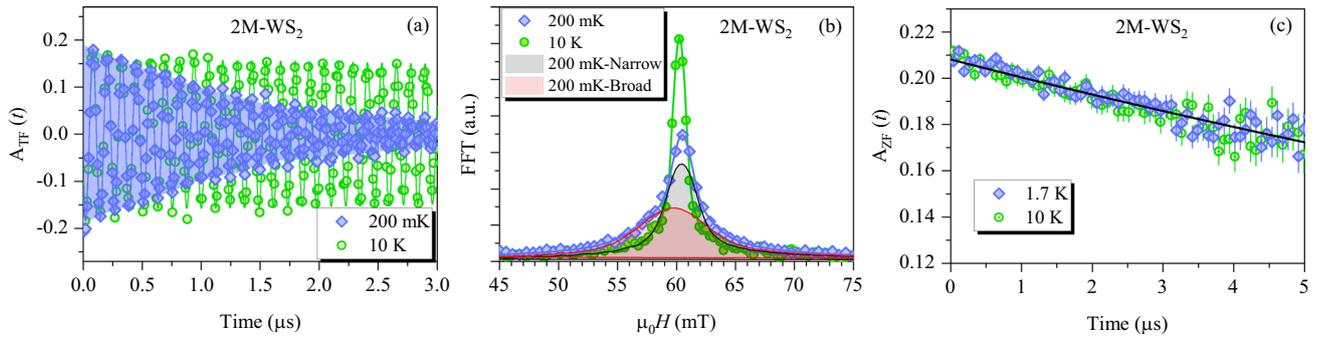


Fig. 1 Transverse-field (TF) and Zero-field (ZF) μ SR time spectra for 2M-WS₂. **a** The TF spectra, above and below T_c are shown. The solid lines represent fits to the data by means of Eq. (1); **b** The Fourier transforms of the μ SR time spectra shown in **a**. **c** ZF μ SR time spectra for 2M-WS₂ recorded above and below T_c . The line represents the fit to the data of the combination of Lorentzian and Gaussian Kubo-Toyabe depolarization function reflecting the field distribution at the muon site created by nuclear dipole moments and randomly oriented diluted weak local electronic moments. Error bars are the s.e.m. in about 10^6 events. The error of each bin count n is given by the s.d. of n . The errors of each bin in $A(t)$ are then calculated by s.e. propagation

trivial surface states. The possible occurrence of topological superconductivity (TSC) in 2M-WS₂ after fine tuning of some parameters is also discussed.³⁵ TSCs are materials with unique electronic states consisting of a full pairing gap in the bulk and gapless surface states composed of Majorana fermions (MFs).^{36–38} Up to now, the only known properties of the superconducting state in 2M-WS₂ are the critical temperatures and fields.³⁵ Thus, a thorough exploration of superconductivity in 2M-WS₂ from both experimental and theoretical perspectives is imperative.

To further study superconductivity and its nature in 2M-WS₂, it is critical to measure the superconducting order parameter at the microscopic level. Thus, we conducted ambient and high-pressure^{39–42} muon spin relaxation/rotation (μ SR) measurements of the magnetic penetration depth λ in the polycrystalline sample of 2M-WS₂. This quantity is one of the fundamental parameters of a superconductor, since it is related to the superfluid density n_s via $1/\lambda^2 = \mu_0 e^2 n_s / m^*$ [where m^* is the effective mass; see also Eq. (2)]. Most importantly, the temperature dependence of λ is particularly sensitive to the topology of the superconducting gap: while in a fully gapped superconductor, $\Delta\lambda^{-2}(T) \equiv \lambda^{-2}(0) - \lambda^{-2}(T)$ vanishes exponentially upon decreasing the temperature, it vanishes as a power of T in a superconductor containing a gap with nodes. The μ SR technique provides a powerful tool to measure λ in the vortex state of type II superconductors in the bulk of the sample,⁴³ in contrast to many techniques that probe λ only near the surface. Details are provided in the Methods section.

Here we show that the superconducting order parameter in 2M-WS₂ possesses single-gap s -wave symmetry, which is consistent with the presence of dominant hole-type charge carriers, as deduced from Hall effect measurements. Moreover, we observed a strong negative pressure effect on the critical temperature T_c and the superconducting gap Δ as well as on the size of the electron pocket around the Γ -point, at which a band inversion appears up to the highest applied pressure. However, the pressure effect on the superfluid density in 2M-WS₂ is very weak. We find that the ratio T_c/n_s is located in the Uemura plot close to those of other superconducting TMD systems, as T_d -MoTe₂ and 2H-NbSe₂, and those of other unconventional superconductors. This suggests that 2M-WS₂ exhibits rather unconventional superconducting properties. The absence of a strong pressure effect on the superfluid density and its correlation with T_c , which was previously found in T_d -MoTe₂ and 2H-NbSe₂, is explained in terms of the absence of competing or cooperating order to superconductivity, as 2M-WS₂ exhibits optimal superconducting conditions already at ambient pressure. By application of pressure we are pushing the system away from any possible competing/cooperating order. Our findings, therefore, pose a challenge for understanding the underlying physics in these layered TMDs and might ultimately

lead to a better understanding of generic aspects of non-BCS behaviors in unconventional superconductors.

RESULTS

Magnetic penetration depth and the superconducting gap symmetry

Figure 1a exhibits transverse-field (TF) muon-time spectra for the polycrystalline sample of 2M-WS₂ measured in an applied magnetic field of $\mu_0 H = 60$ mT above ($T = 10$ K) and below ($T = 200$ mK) the superconducting (SC) transition temperature T_c . Above T_c the oscillations reflecting the muon-spin precession show a small damping due to the random local fields from the nuclear magnetic moments. Below T_c the relaxation rate strongly increases upon decreasing the temperature due to the presence of a nonuniform local magnetic field distribution resulting from the formation of the flux-line lattice (FLL) in the Shubnikov phase. By carefully examining the TF- μ SR data, we find that the sample consists of a superconducting and a non-superconducting volume fraction. To visualise these two fractions of the sample, we report on Fig. 1b the Fourier transforms of the μ SR time spectra, shown in Fig. 1a. At $T = 200$ mK the narrow signal around $\mu_0 H_{\text{ext}} = 60$ mT, originates from the non-superconducting part of the sample, while the broad signal with a first moment $\mu_0 H_{\text{int}} < \mu_0 H_{\text{ext}}$, marked by the solid arrow in Fig. 1b, arises from the superconducting part of the sample. The estimated superconducting volume fraction from the μ SR data is $\sim 45\%$. It is interesting to investigate whether magnetism is present either in the superconducting or non-superconducting fractions of the sample. In order to search for magnetism, we have carried out zero-field (ZF) μ SR experiments above and below T_c , which are shown in Fig. 1c. No sign of static magnetism could be detected in the ZF time spectra down to 1.7 K. Moreover, the ZF relaxation rate is small and does not change between 10 and 1.7 K. ZF- μ SR spectra are well described by the combination of a Lorentzian and a Gaussian Kubo-Toyabe depolarization function,^{44,45} reflecting the field distribution at the muon site created by the nuclear dipole moments and randomly oriented diluted weak local electronic moments. Returning to the discussion of the TF- μ SR data, we observe a strong diamagnetic shift of the internal magnetic field $\mu_0 H_{\text{int}}$ sensed by the muons below T_c . This is evident in Fig. 2a, where we plot the temperature dependence of $\Delta B_{\text{dia}} = \mu_0(H_{\text{int,SC}} - H_{\text{int,NS}})$, i.e., the difference between the internal field $\mu_0 H_{\text{int,SC}}$ measured in the SC fraction and one $\mu_0 H_{\text{int,NS}}$ measured in the normal state at $T = 10$ K. The strong diamagnetic shift along with the negative field dependence of the superconducting depolarization rate σ_{SC} (see Fig. 2b) excludes the occurrence of field induced magnetism in 2M-WS₂. Note that in some Fe-based and cuprate high temperature

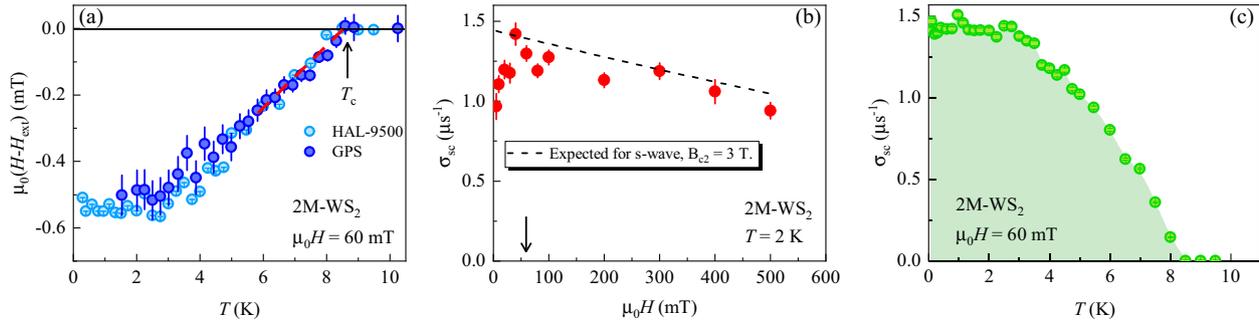


Fig. 2 Superconducting muon spin depolarization rate σ_{sc} and the diamagnetic shift for 2M-WS₂. **a** The temperature dependence of the diamagnetic shift $\Delta B_{dia} = \mu_0(H_{int,SC} - H_{int,NS})$ in an applied magnetic field of $\mu_0H = 60$ mT. The arrow denotes T_c . The data taken on HAL-9500 μ SR spectrometer, equipped with BlueFors vacuum-loaded cryogen-free dilution refrigerator (DR) and on the standard GPS spectrometer are shown. **b** Field dependence of the muon spin relaxation rate $\sigma_{sc}(T)$ at 1.6 K. Arrow indicates the field value at which the temperature dependent measurements were carried out. Dashed line shows the theoretical field dependence expected for the *s*-wave superconductor, taking into account the critical field of 3 T. **c** The temperature dependence of $\sigma_{sc}(T)$. The error bars represent the s.d. of the fit parameters

superconductors, where field induced magnetism was detected, a paramagnetic shift and a linear increase of σ_{sc} with magnetic field were observed.^{46–48} The absence of magnetism in zero-field or under applied magnetic fields implies that the increase of the TF relaxation rate below T_c is solely arising from the FLL in the superconducting fraction. The strong superconducting response from nearly 50% of the sample points to the bulk superconductivity in 2M-WS₂. We note that the diamagnetic moment, which we deduce from the bulk magnetization measurements suggest a 100% SC volume in the sample, which is consistent with the previous report.³⁵ However, bulk magnetisation measures the diamagnetic screening of the whole sample where a 100% screening does not necessarily imply a 100% SC volume. μ SR, being a local probe, directly measures the SC volume fraction within the sample. Thus, in this work we provide a more precise estimate for the SC volume in 2M-WS₂. The μ SR evidence for a phase separation between SC and paramagnetic regions in 2M-WS₂ is an interesting finding, which might be an intrinsic feature of this system.

From the TF muon time spectra, we determined the Gaussian superconducting relaxation rate σ_{sc} (after subtracting the nuclear contribution), which is proportional to the second moment of the field distribution (see Methods section). Figure 2b shows the obtained field dependence of σ_{sc} at 1.7 K. Each point was obtained by field cooling the sample from above T_c to 1.7 K. As expected from the London model one observes that first σ_{sc} strongly increases with increasing magnetic field until reaching a maximum at 40 mT.⁴⁹ Above 40 mT, σ_{sc} decreases with increasing magnetic field. This appears consistent with a behaviour expected for *s*-wave superconductor for an ideal triangular vortex lattice.⁴⁹ Taking into account the critical field of 3 T, the theoretical *s*-wave behaviour has been calculated according to the Brandt formula.⁴⁹ It is shown by the dashed line in Fig. 2b, which agrees well with the experimental data. The second moment of the resulting inhomogeneous field distribution is related to the magnetic penetration depth λ by $\langle \Delta B^2 \rangle \propto \sigma_{sc}^2 \propto \lambda^{-4}$.⁴⁹ In order to investigate the symmetry of the superconducting gap, we have therefore derived the temperature-dependent London magnetic penetration depth $\lambda(T)$, which is related to the relaxation rate by:

$$\frac{\sigma_{sc}(T)}{\gamma_\mu} = 0.06091 \frac{\Phi_0}{\lambda^2(T)}. \quad (1)$$

Here, γ_μ is the gyromagnetic ratio of the muon, and Φ_0 is the magnetic-flux quantum. In order to accurately determine the temperature dependence of λ , it is important to do the temperature dependent measurements of σ_{sc} slightly above the maximum of $\sigma_{sc}(H)$, where Eq. (1) is valid. Thus, the measurements were done

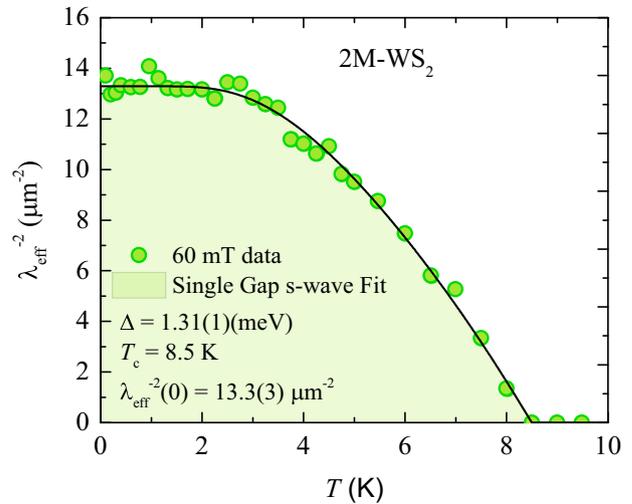


Fig. 3 Temperature evolution of λ^{-2} for 2M-WS₂. **a** The temperature dependence of λ^{-2} measured at ambient pressure. The solid line represents a fit using a single gap *s*-wave model. The error bars are calculated as the s.e.m

with an applied magnetic field of 60 mT. In Fig. 2c, we show the temperature dependence of the muon spin depolarization rate σ_{sc} . Below T_c the relaxation rate σ_{sc} starts to increase from zero with decreasing temperature due to the formation of the FLL and reaches $\sigma_{sc} \simeq 1.43 \mu s^{-1}$ at the base-*T*. The temperature dependence of σ_{sc} which reflects the topology of the SC gap, exhibits a saturation at low temperatures. This is consistent with a nodeless superconductor, for which the superfluid density $n_s \propto \sigma_{sc}$ reaches its zero-temperature value exponentially. For a quantitative analysis, we in the local (London) approximation ($\lambda \gg \xi$, where ξ is the coherence length), calculated $\lambda(T)$. The result of the gap analysis is shown in Fig. 3. The data are perfectly compatible with a single *s*-wave gap with a value of $\Delta = 1.31(1)$ meV.

The London magnetic penetration depth λ is given as a function of n_s ,⁵⁰ the effective mass m^* , ξ and the mean free path l , according to

$$\frac{1}{\lambda^2} = \frac{4\pi n_s e^2}{m^* c^2} \cdot \frac{1}{1 + \xi/l}. \quad (2)$$

For systems close to the clean limit, $\xi/l \rightarrow 0$, the second factor essentially becomes unity, and the simple relation $1/\lambda^2 \propto n_s/m^*$ holds. Considering the upper critical fields H_{c2} of 2M-WS₂, as reported in detail by Fang et al.,³⁵ we can estimate the in-plane

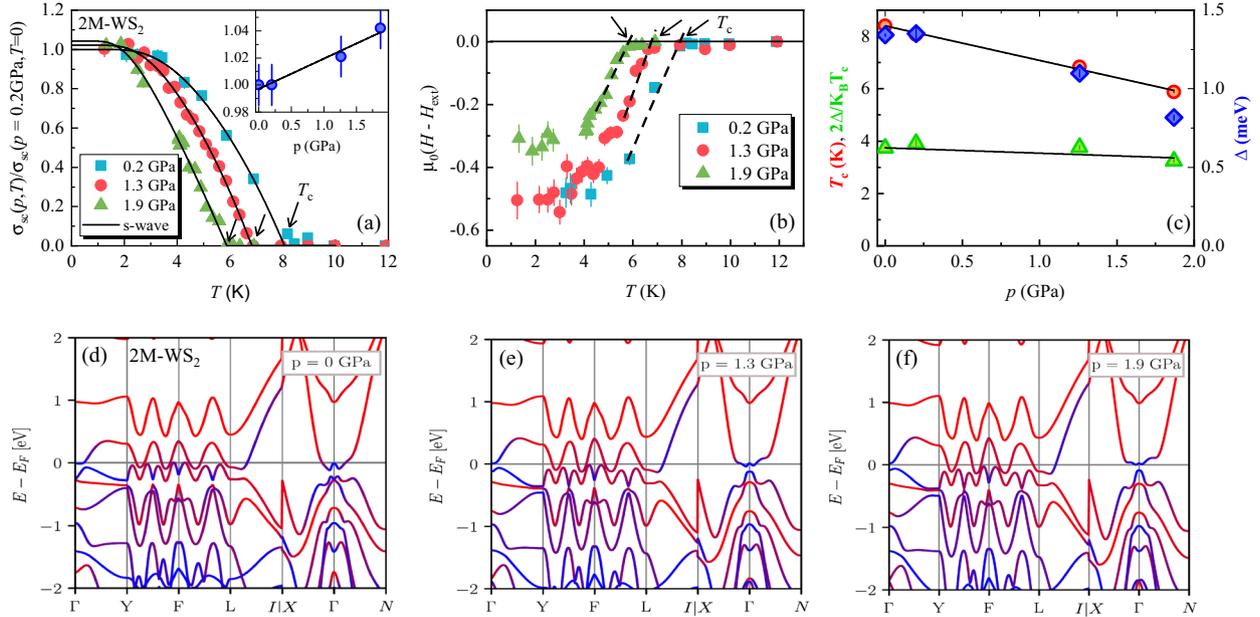


Fig. 4 Pressure evolution of various quantities. **a** The temperature dependence of $\sigma_{sc}(T)$, normalized to its value for the lowest applied pressure, under various applied pressures. The inset illustrates the weak positive pressure dependence of σ_{sc} . **b** The temperature dependence of the diamagnetic shift $\Delta B_{dia} = \mu_0(H_{int,SC} - H_{int,NS})$, recorded for various hydrostatic pressures. **c** Pressure dependence of the superconducting transition temperature T_c , the zero-temperature value of the superconducting gap Δ and the ratio $2\Delta/k_B T_c$ for 2M-WS₂. The error bars represent the s.d. of the fit parameters. Band structure in the presence of spin-orbit coupling for $p = 0$ GPa **d**, 1.3 GPa **e** and 1.9 GPa **f**. Red color corresponds to d orbitals of W atoms, while the blue color indicates the p orbitals of S atoms

coherence length to be $\xi_{ab} \approx 8.8$ nm at ambient pressure. At ambient pressure, the in-plane mean free path l was estimated to be $l_{ab} \approx 200$ nm. No estimates are currently available for l under pressure. However, the in-plane l is most probably independent of pressure considering the fact that the pressure mostly reduces the interlayer distance due to the unique anisotropy resulting from the stacking of layers with van der Waals type interactions between them. Thus, in view of the short coherence length and relatively large l , we can reliably assume that 2M-WS₂ lies close to the clean limit.^{23,51} With this assumption, we obtain the ground-state value $n_s/(m^*/m_e) \approx 2.8 \times 10^{26} \text{ m}^{-3}$, where m_e is the free electron mass.

Probing superconductivity and band structure as a function of pressure

To gain further insight into the superconducting properties of 2M-WS₂, the temperature dependence of the superfluid response was measured under applied pressures up to 1.9 GPa. Moreover, the pressure effect of the electronic structure was also calculated. We note that the SC volume fraction was found to be independent of pressure. In Fig. 4a, b, we show the temperature evolution of σ_{sc} , normalised to the value at ambient pressure, and the diamagnetic shift ΔB_{dia} measured under various hydrostatic pressures. A single gap s -wave model describes the $\sigma_{sc}(T)$ data very well up to the highest pressure. Remarkably, both T_c and Δ decreases substantially upon application of pressure. T_c decreases from 8.5 K at $p = 0$ GPa to 6 K at 1.9 GPa. Δ decreases from 1.31(1) meV at 0 GPa to 0.82(2) meV at 1.9 GPa. However, the analysis of the temperature dependence of $\sigma_{sc}(T)$ reflects only a $\sim 5\%$ increase of the zero-temperature value of n_s . This means that the absolute value of the superfluid density in 2M-WS₂ is very weakly affected by pressure. The band structures, calculated in the presence of the spin-orbit coupling for ambient pressure and under the applied pressures of $p = 1.3$ GPa and 1.9 GPa are shown in Fig. 4d–f (see also Fig. S1 in the Supplementary Information). The band inversion between the p -orbital of the S atoms and the d -orbital of the W atoms at the Γ -point is found up to the highest investigated pressure. This

indicates that the topology of the bands in 2M-WS₂ remains nontrivial under pressure. We also find that the electron pockets at the Γ -point shrink upon application of pressure, which might have some interesting consequences on the physical properties of the system.

DISCUSSION

We can now discuss the main results of our measurements on 2M-WS₂:

- (i) The temperature dependence of the superfluid density, reflected by the one of the relaxation rate σ_{sc} , is well described at all pressures by a single gap s -wave model. This is surprising since a multi-band bulk electronic structure with hole-like bands around the N point and electron-like bands around the Γ point was found for 2M-WS₂. On the other hand, Hall effect measurements showed that the hole-type carriers are dominant with a very high density of $n_{e,h} = 8.58 \times 10^{26} \text{ m}^{-3}$ at $T = 10$ K. It is interesting that the superfluid density $n_s/(m^*/m_e) \approx 2.8 \times 10^{26} \text{ m}^{-3}$, which we estimated for 2M-WS₂ is very close to the normal state hole density $n_{e,h}$, indicating that the superconductivity stems mostly from hole carriers. Thus, single gap superconductivity in this multi-band system may be explained by the fact that the superconducting gap occurs only on the hole-like Fermi surface and that the carrier density on the electron Fermi surface is not sufficient to induce superconductivity. This conclusion is also substantiated by the fact that superfluid density is insensitive to the shrinkage of the electron pocket, caused by pressure. If superconductivity would exist on the electron pocket, the pressure induced reduction of the size of the electron pocket would result to the reduction of the associated electron carrier concentration and thus the reduction of the superfluid density, which is not the case in 2M-WS₂. Single gap s -wave superconductivity in 2M-WS₂ is also different from the two-gap $s + s$ -wave superconductivity, observed in the superconducting TMDs T_d -MoTe₂ and

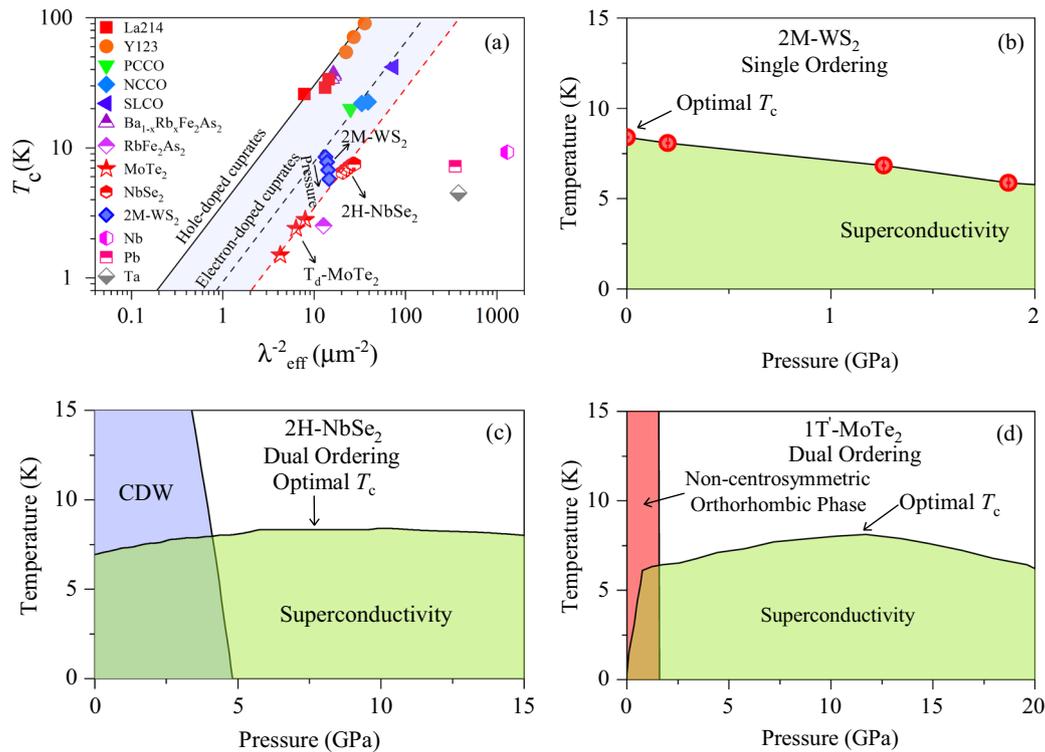


Fig. 5 Superfluid Density versus T_c and comparison between the phase diagrams. **a** A plot of T_c against the $\lambda^{-2}(0)$ obtained from our μSR experiments in 2M-WSe_2 , 2H-NbSe_2 and MoTe_2 . Data points for MoTe_2 and 2H-NbSe_2 are taken from refs. ^{23,24}. The dashed red line represents the linear fit to the MoTe_2 and 2H-NbSe_2 data. Uemura relation for hole and electron-doped cuprates are shown as solid ^{25,26,28} and dashed lines, ³⁰ respectively. Few points for cuprate and Fe-based superconductors are shown. The points for various conventional BCS superconductors are also shown. The temperature-pressure phase diagram for 2M-WSe_2 **b**, showing only the superconducting order. The schematic temperature-pressure phase diagrams for 2H-NbSe_2 **c** (after ref. ⁵³) and MoTe_2 (after ref. ⁵) **d**, exhibiting dual ordering

2H-NbSe_2 . This again might be related to the fact that in both these systems both hole and electron bands contribute to superconductivity, while in 2M-WSe_2 the superconductivity most likely arises predominantly from the hole like band. Regarding the surface states, a single Dirac cone at the Γ point was reported. When the Fermi level is exactly at the Dirac point, only a single Fermi surface was obtained.³⁵ A single Fermi surface at the surface and a dominant hole-like Fermi surface in the bulk is consistent with single gap superconductivity, observed in our study. It was also suggested that if the superconductivity is induced on this single Fermi surface, topological superconductivity is expected. As the muons penetrate deep into the material, we cannot obtain information on the superconductivity on the surface and about its topological nature. However, because of the semimetallic bulk electronic structure, the topological surface states are partially mixed with bulk states. Thus, the superconducting properties in the bulk could, to some extent, reflect the properties also on the surface.

- (ii) We observed, for the first time, a strong negative pressure effect on the critical temperature T_c and the superconducting gap Δ . Both quantities decrease by $\sim 30\%$ under 1.9 GPa. Note that the superconducting transition temperature, estimated by the Allen and Dynes modified McMillan formula,³⁵ was found to be $\sim 2\text{K}$, which is a factor of 4 smaller than the experimental value $T_c \approx 8.5\text{K}$ (see Fig. S2 in the Supplementary Information). This indicates that some dynamical and anharmonic effects on the electron-phonon coupling as well as interband scattering between electron and hole pockets are most likely the reasons for high- T_c in 2M-WSe_2 . According to our DFT calculations, the electron

pocket around the Γ point shrinks by pressure, which would lead to the suppression of interband processes and this might have some effect on T_c . Pressure could also weaken the anharmonic electron-lattice interactions, giving rise to the suppression of T_c . Some additional experiments are certainly needed to understand the negative pressure effect on the critical temperature. The superfluid density $n_s/(m^*/m_e)$ is essentially pressure independent, displaying at the most a slight increase of about 5%. The ratio between the superfluid density and the critical temperature is located in the Uemura plot close to those of $T_d\text{-MoTe}_2$ and 2H-NbSe_2 and other unconventional superconductors, as shown in Fig. 5. This suggests that 2M-WSe_2 exhibits rather unconventional SC properties and might suggest a common mechanism and related electronic origin for the superconductivity in these superconducting TMDs. On the other hand, the insensitivity of the superfluid density to the strong change in T_c is in contrast to the strong correlation between these two quantities in $T_d\text{-MoTe}_2$ and 2H-NbSe_2 . Let us try to understand this apparent discrepancy. The nearly linear relationship between T_c and the superfluid density was originally observed in hole-doped cuprates in the underdoped region of the phase diagram,^{25,26} where the ratio between T_c and their effective Fermi temperature T_F is about $T_c/T_F \sim 0.05$ corresponding to a 4–5 times reduction of T_c from the ideal Bose condensation temperature for a non-interacting Bose gas. These results were discussed in terms of a crossover from Bose-Einstein condensation to BCS-like condensation.²⁸ It is important to note that in cuprates the relationship between T_c and $n_s/(m^*/m_e)$ was shown to depend on which part of the SC dome the samples are located. Thus, the left-side of the dome (underdoped), which

has close proximity with the competing/cooperating anti-ferromagnetic phase, the center of the dome (optimally doped), which is away from the AFM phase or the right side of the dome (overdoped) region, which is clearly separated from the AFM phase. The linear increase of T_c with $n_s/(m^*/m_e)$ is observed only in the underdoped region of the phase diagram. Within the optimal doping region T_c does not change despite the fact that $n_s/(m^*/m_e)$ increases. In the overdoped region, T_c decreases, but $n_s/(m^*/m_e)$ shows a small increase only. A similar behaviour was also observed in Fe-based superconductors.⁵² With this in mind, we compare the temperature-pressure phase diagrams for the systems 2M-WS₂, T_d-MoTe₂, 2H-NbSe₂. The phase diagrams are shown in Fig. 5b–d. There are two obvious differences between the phase diagrams. In the case of 2H-NbSe₂ and T_d-MoTe₂ (Fig. 5c, d), the phase diagram consists of two different orders at ambient pressure: superconductivity and either charge density wave order or non-centrosymmetric structural order. In addition, T_c of both systems increases with increasing pressure within the investigated pressure region (0–2 GPa), indicating that the samples are located in the left-hand side of the dome with close proximity to another phase. In the case of 2M-WS₂ (Fig. 5b), the system has solely superconducting order and there is no additional competing/cooperating order. In addition, the system 2M-WS₂ has the highest T_c at ambient pressure, suggesting that the system is already in its optimal conditions in terms of superconductivity. Upon application of pressure, T_c decreases substantially, pushing the system towards the right-hand side of the dome, i.e. pushing it even further away from any possible competing phase. So, the location of 2M-WS₂ in the optimal (ambient pressure) and above the optimal (under pressure) superconducting regions of the phase diagram might be a reason for the absence of the correlation between the superfluid density and the critical temperature in this system.

In conclusion, using DFT, we show that the topology of the bands in 2M-WS₂ remains nontrivial up to the highest applied pressure. We further provide the first microscopic investigation of the superconductivity in the layered superconductor 2M-WS₂ at ambient pressure as well as under hydrostatic pressures by means of muon-spin rotation. Specifically, the zero-temperature magnetic penetration depth $\lambda(0)$ and the temperature dependence of the superfluid density were studied in 2M-WS₂ by means of μ SR experiments with pressures up to $p \simeq 1.9$ GPa. The temperature dependence of the superfluid density λ^{-2} is well described by a single gap *s*-wave scenario with a gap value of $\Delta \simeq 1.31(1)$ meV at ambient pressure. Considering the previous observations of the dominant hole-like Fermi surface in the bulk and single Fermi surface on the surface we suggest that the well resolvable SC gap occurs only on the hole-like Fermi surface. We also find that the ratio T_c/n_s is located in the Uemura plot close to those of T_d-MoTe₂ and 2H-NbSe₂ and other unconventional superconductors, suggesting that 2M-WS₂ exhibits non-standard SC properties. Moreover, we observed the strong negative pressure effect on T_c and Δ , which may partly be due to the reduction of the size of the electron pocket at the Γ point, at which a band inversion appears up to the highest applied pressure. The superfluid density shows only a very weak positive pressure effect and thus the correlation between the superfluid density and the critical temperature is absent in 2M-WS₂. This is in contrast to the strong pressure effects on λ^{-2} and its correlation with T_c , observed in the superconducting TMDs T_d-MoTe₂ and 2H-NbSe₂. This discrepancy is discussed in terms of the absence of competing or cooperating order to superconductivity in 2M-WS₂. These results hint towards the complex nature of the superconductivity in TMDs, despite its

s-wave nature, which might have far reaching consequences for the future development of devices based on these materials.

METHODS

Sample preparation

Topochemical synthesis procedure of the metastable, monoclinic tungsten diselenide (2M-WS₂) can be found elsewhere.^{35,54} In a first step, a hexagonal phase of 2M-WS₂ (SG P6₃/mmc - No 194), was synthesized by solid state reaction method at 850 °C for 35 h from a stoichiometric mixture of elemental sulfur (5N, Alfa Aesar) and tungsten (5N, Alfa Aesar). Then potassium intercalation and growth of KWS₂ was conducted by annealing the stoichiometric mixture of K (3N5, Aldrich) and 2M-WS₂ at 850 °C. After 35 h a specimen was cooled down to 550 °C with a rate of 6 °C/h. All syntheses reactions and sample growth processes described above were conducted in a double wall, evacuated and sealed quartz ampules. In a third step K_x(H₂O)_yWS₂ compound was created by washing 3 g of KWS₂ with deionized water. Finally K_x(H₂O)_yWS₂ was oxidized with 200 ml of 0.1N K₂Cr₂O₇/0.1N H₂SO₄ aqueous solution in order to get polycrystalline samples of 2M-WS₂. Powders from the same batch were pressed in the form of pellets and were measured with various instruments. For the low background GPS instrument and low-temperature HAL-9500 instrument, equipped with BlueFors vacuum-loaded cryogen-free dilution refrigerator (DR), we used one pellet with 10 mm in diameter. For high pressure GPD instrument, several pellets with 5.9 mm in diameter were prepared and placed inside the pressure cell.

Pressure cell

Double wall piston-cylinder type of cell made of CuBe/MP35N material was used in μ SR experiments to generate pressures up to 1.9 GPa.^{39–42} Small indium plate was placed together with the sample in the pressure cell filled with the Daphne oil. The pressure was estimated by tracking the SC transition of a indium plate by AC susceptibility. The filling factor of the pressure cell was maximised. The fraction of the muons stopping in the sample was $\sim 45\%$. The background of the pressure cell is well known and characterised.³⁹

μ SR experiment

Spin-polarized muons μ^+ are extremely sensitive magnetic probes. Muon-spin experiences the Larmor precession either in the local field or in an applied magnetic field. By probing the field distribution in the vortex state of a Type-II superconductor using transverse field μ SR technique, fundamental parameters such as the magnetic penetration depth λ and the coherence length ξ can be measured in the bulk of a superconductor.

Analysis of TF- μ SR data

The following function is used to analyse the TF μ SR data:^{55,56}

$$P(t) = A_s \exp\left[-\frac{(\sigma_c^2 + \sigma_{nm}^2)t^2}{2}\right] \cos(\gamma_\mu B_{int,s}t + \varphi) + A_{pc} \exp\left[-\frac{\sigma_{pc}^2 t^2}{2}\right] \cos(\gamma_\mu B_{int,pc}t + \varphi), \quad (3)$$

Here A_s and A_{pc} are the initial asymmetries of the μ SR signal for the sample and the pressure cell, respectively. $\gamma/(2\pi) \simeq 135.5$ MHz/T is the muon gyromagnetic ratio and φ is the initial phase of the muon-spin ensemble. B_{int} is the internal magnetic field at the muon site. The depolarization rate σ_c is due to the formation of the flux line lattice in the SC state and σ_{nm} describes the damping due to the nuclear dipolar contribution. σ_{nm} was obtained above T_c and was assumed to be constant over the entire temperature range. The relaxation rate σ_{pc} reflects the depolarization due to the nuclear moments of the pressure cell. It exhibits the temperature dependence below T_c ⁴¹ due to the influence of the diamagnetic response of the SC sample on the pressure cell. In order to consider this influence we assume a linear coupling between σ_{pc} and the field shift of the internal magnetic field in the SC state: $\sigma_{pc}(T) = \sigma_{pc}(T > T_c) + C(T)(\mu_0 H_{int,NS} - \mu_0 H_{int,SC})$, where $\sigma_{pc}(T > T_c) = 0.25 \mu s^{-1}$ is the temperature independent relaxation rate. $\mu_0 H_{int,NS}$ and $\mu_0 H_{int,SC}$ are the internal magnetic fields measured in the normal and in the SC state, respectively.

Analysis of $\lambda(T)$

$\lambda(T)$ was calculated within the London approximation ($\lambda \gg \xi$) by the following function:^{50,55}

$$\frac{\lambda^{-2}(T, \Delta_{0,i})}{\lambda^{-2}(0, \Delta_{0,i})} = 1 + \frac{1}{\pi} \int_0^{2\pi} \int_{\Delta_i(T, \varphi)}^{\infty} \left(\frac{\partial f}{\partial E} \right) \frac{E dE d\varphi}{\sqrt{E^2 - \Delta_i(T, \varphi)^2}}, \quad (4)$$

where $f = [1 + \exp(E/k_B T)]^{-1}$ is the Fermi function, φ is the angle along the Fermi surface, and $\Delta_i(T, \varphi) = \Delta_{0,i} f(T/T_c) g(\varphi)$ ($\Delta_{0,i}$ is the maximum gap value at $T=0$). The temperature dependence of the gap is given by the expression $\Gamma(T/T_c) = \tanh\{1.82[1.018(T_c/T - 1)]^{0.51}\}$,⁵⁷ while $g(\varphi)$ describes the angular dependence of the gap. $g(\varphi) = 1$ for both an s -wave and an $s + s$ -wave gap, and $g(\varphi) = |\cos(2\varphi)|$ for a d -wave gap.

DFT calculations

2M-WS₂ crystal has a monoclinic structure with the space group symmetry $C_{2/m}$ (number 12) and the following lattice parameters $a = 12.856 \text{ \AA}$, $b = 3.2257 \text{ \AA}$, $c = 5.7109 \text{ \AA}$, $\alpha = \gamma = 90^\circ$ and $\beta = 112.942^\circ$ (crystallographic data CCDC 1853656). Full-relativistic electronic structure calculations were performed in Vienna *ab initio* simulation package (VASP)^{58,59} using Perdew–Burke–Ernzerhof (PBE)^{60,61} generalized gradient approximation (GGA) exchange–correlation functional and projected augmented wave (PAW) potentials.^{62,63} The van der Waals interactions were taken into account within the DFT-D2 approach by Grimme.⁶⁴ The plane wave basis cutoff was set to 600 eV and $9 \times 9 \times 9$ k-points grids were generated within Monkhorst–Pack method.

DATA AVAILABILITY

All relevant data are available from the authors. The data can also be found at the following link <http://musruser.psi.ch/cgi-bin/SearchDB.cgi> using the following details: Area: HAL and GPD. Year: 2018. Run numbers: 1009–1042 for HAL and 3199–3281 for GPD.

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AUTHOR CONTRIBUTIONS

Project planning and coordination: Z.G. Sample growth and XRD experiment: D.G. and E.P. μ SR experiments: Z.G., R.K., J.V., H.L., A.A. μ SR data analysis: Z.G. Magnetization measurements: F.v.R. DFT calculations: M.B., S.S.T. and T.N. Data interpretation and draft writing: Z.G. with contributions and comments from all authors.

ADDITIONAL INFORMATION

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